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ABSTRACT

We examine whether annual, quarterly, and monthly U.S. aggregate consumption data could have been generated by a utility maximizing representative agent with intertemporally separable utility. The model appears inapplicable over the full time periods covered by the NIPA data, which are the sample periods often used in the literature. The model does appear applicable, however, over long subsamples. The data also are inconsistent with separability assumptions routinely made in the literature. In particular, the main categories of consumption (nondurables, services, and durables) are not mutually separable. We consider the implications of our results for inference about consumption based on the representative agent model.
"To assume that the representative agent acts like an ideal consumer is a hypothesis worth testing: to assume that an actual person, the Mr. Brown or Mr. Jones who lives round the corner, does in fact act in such a way does not deserve a moment's consideration." Hicks (1956, p.55, A Revision of Demand Theory)

1. INTRODUCTION

The representative agent model is a popular approach to analyzing aggregate consumption. Its basic assumption is that one can treat the aggregate data as the outcome of a single "representative" consumer's decisions. However, the conditions on individual preferences necessary for the representative agent to be an exact representation of the behavior of underlying agents are quite stringent, so much so as to be implausible. Most criticism of the representative agent paradigm arises from this problem; for example, see Kirman (1992). Nonetheless, the representative agent model can be useful even without a complete micro-foundation. A central task of macroeconomics is to explain aggregate data and make predictions. The representative agent model is useful if it helps do so. Exact aggregation of individual preferences is not essential. What is essential is that there exists some "representative" utility function consistent with the data, for only then can the researcher resort to standard utility theory in conducting his analysis.

The usual approach is to assume that a representative utility function exists and that it satisfies certain separability restrictions permitting analysis of convenient subsets of the data. Empirical results then are interpreted in terms of individual behavior, and any statistical rejection of the model is treated as evidence of the misspecification of the representative agent's utility function. See, for example, the recent survey by Kocherlakota (1996). Another possibility, however, is that no representative utility function with the implied separability structure exists. Then subsequent interpretations of results in terms of individual behavior are suspect at best, and empirical rejections might reflect invalidity of the entire representative agent approach rather than merely misspecification of that agent's utility function.

One can check whether a representative agent utility function exists by using Varian's (1982, 1983) tests of whether a set of data is consistent with the Generalized Axiom of Revealed Preference (GARP). Consistency with GARP is necessary and sufficient for existence of a well-behaved utility function capable of generating the data. An important advantage of Varian's approach is that the tests are non-parametric and so require only mild
assumptions on the form of the utility function.

We use Varian’s tests to see if a representative agent utility function exists for the monthly, quarterly and annual aggregate consumption data of the United States.¹ The tests require user costs for the durable goods, which are unavailable in official statistics. We therefore construct measures ourselves, which requires assumptions about the expectation mechanism of the representative agent. We tried several expectations models, but the results are not very sensitive to which of those is used. We start by testing whether the data are consistent with a well behaved intertemporally separable utility function. We find that the data generally are not consistent with such a function over the full periods for which the data are available. Those are the sample periods often used in previous empirical work. However, we can identify the periods responsible for the violations and thus uncover subsamples of the data over which GARP is satisfied. We find that there are long subsamples of both the annual and quarterly data that are consistent with GARP, and the subsamples for the two kinds of data are essentially the same. In particular, 1981 is the only year of instability for both the annual and quarterly data. In contrast, the monthly data show a great many violations of GARP. The subsamples of monthly data consistent with GARP are so short that estimation of the utility function is likely to be impractical.

Having identified periods over which GARP holds, we explore the structure of the representative utility function within these periods. We apply Varian's (1982, 1983) separability tests to several possible groupings of aggregate consumption’s components, such as furniture, clothing, automobiles, and so forth. Again, the annual and quarterly data yield very similar results. Our results support the analysis of nondurables and services as a group without the inclusion of durables. However, if all three categories are analyzed at once, then durables must be divided into certain subgroups. Interestingly, our results indicate automobiles should be treated as a separate subgroup, as recently advocated by Wilcox (1992) after his analysis of the survey methods by which the data are collected.

An outline of the paper is as follows. Section 2 describes the theory behind Varian’s tests and discusses

¹See Swofford and Whitney (1987, 1988), Manser and McDonald (1988) and Browning (1989) for pioneering work in applying GARP tests to aggregate consumption data. These studies have some limitations that we discuss below. Belongia and Chalfant (1989) use the GARP tests to study the empirical definition of money, and Chalfant and Alston (1988) have used them to study changes in tastes for meat.
the properties of the tests. Section 3 describes the data used in our study and in particular the calculations needed to construct price variables for durable goods. Section 4 contains the results and Section 5 concludes with a discussion of some implications of our results.

2. TESTING GARP AND THE SEPARABILITY STRUCTURE OF THE UTILITY FUNCTION

The standard representative agent model supposes the agent maximizes his lifetime utility,

\[
E_0 \left[ \sum_{t=0}^{\infty} u(x_t)(1+r)^{-t} \right]
\]

subject to his lifetime budget constraint

\[
\sum_{t=0}^{\infty} p_t x_t (1+r)^{-t} = A_0 + \sum_{t=0}^{\infty} y_t (1+r)^{-t}
\]

where \( u \) is the aggregate intratemporal utility function, \( x_t \) is a k-vector of goods \( \{x_t\} \), \( p_t \) is a corresponding vector of relative prices, \( A_0 \) is initial financial assets, \( y_t \) is real labor income (here taken as exogenous for simplicity), \( r \) is the real interest rate, \( \rho \) is the rate of time preference, \( T \) is the time horizon and \( E_t[.] \) denotes expectations conditional on information at time 0. Possible sources of uncertainty include \( y \), \( r \), and \( T \). Notice that representative agent's utility function is assumed to be intertemporally separable. This restriction is imposed in many of the models underpinning macroeconomic analysis of consumption. However, it rules out such features as habit formation; we return to this issue in Section 5.

Whether the foregoing model is appropriate for analyzing aggregate consumption data is an empirical question that can be addressed with Varian's (1982, 1983) procedures for testing consistency with GARP. We therefore begin with a brief review of those tests and their background.

1. Testing GARP. GARP is simply a mild generalization of the Strong Axiom of Revealed Preference (SARP) that allows "flat spots" in the preference relation, so that the marginal rate of substitution can be constant along a section of the indifference curve. Precise statements of SARP and GARP are given in Appendix 1. GARP's importance here is that we can use it to see if there is a utility function that could have generated a given set of data.

Suppose we have \( T \) observations on the k-vector \( x_t \) of consumption goods and on its corresponding k-vector of prices, \( p_t \). The following definition is from Varian (1983).
DEFINITION: RATIONALIZING UTILITY FUNCTION. A utility function \( u \) rationalizes the data \( \{x_t, p_t\} \), \( t=1, \ldots, T \), if \( u(x_t) \geq u(z) \) for all \( z \) such that \( p_t x_t \geq p_t z \) for all \( t \).

This definition simply means that \( u(.) \) is consistent with the data if observed consumption would be optimal under \( u(.) \). Varian (1982) develops methods for examining whether any such utility function exists for a given data set based on the following theorem due to Afriat (1967) and Diewert (1973):

AFRIAT'S THEOREM. The following conditions are equivalent.

1. There exist numbers \( U_t, \lambda_t > 0 \) that satisfy the Afriat inequalities
   \[ U_t - U_s + \lambda_t p_t (x_t - x_s) \]
   for \( s, t = 1, \ldots, T \).
2. The data satisfy GARP.
3. There exists a nonsatiated utility function that rationalizes the data.
4. There exists a concave, monotonic, continuous, nonsatiated utility function that rationalizes the data.

By parts 3 and 4 of the theorem, if there is a utility function that rationalizes the data, it will have the properties typically assumed in consumer theory. By parts 2 and 3, some rationalizing utility function exists if and only if the data satisfy GARP. By parts 1 and 2, we can test for GARP by seeing if there is a set of numbers \( \{U, \lambda\} \) satisfying a set of linear inequalities. It is a straightforward linear programming exercise to see if an appropriate set \( \{U, \lambda\} \) exists.\(^2\) That exercise provides the method for testing if the data satisfy GARP: simply check if the "Afriat numbers" \( \{U, \lambda\} \) exist. Note that Afriat's Theorem says GARP is equivalent to the existence of a rationalizing utility function. Therefore, if Afriat numbers cannot be found for the data, a rationalizing utility function does not exist.

2. Testing Separability Assumptions. Suppose the consumption data satisfy GARP. We then know there is some utility function \( u(x) \) that rationalizes the data. However, that function has as its argument the entire \( k \)-vector of consumption goods \( x \), and analysis of consumption behavior is inconvenient or even intractable if \( k \) is large. We can solve this problem by aggregating the elements of \( x \) into various subgroups of expenditures.\(^3\) The question is

\(^2\)The numbers \( U \) and \( \lambda \) can be interpreted as the utility levels and marginal utilities of income at the observed demands. The inequality in part 1 follows directly from the concavity of the utility function and the first-order conditions of utility maximization. See Varian (1982, 1983).

\(^3\)Note that there are two kinds of aggregation going on. Because we are talking about a representative consumer, the elements of \( x \) - that is, the individual consumption goods - already have been aggregated across households. We
which elements of \( x \) can be combined legitimately into a particular group. That questions also can be addressed with GARP tests. To see how, we need another definition and another theorem.

Suppose the vector \( x \) is partitioned into two sets \( a = (x_1, \ldots, x_m) \) and \( b = (x_{m+1}, \ldots, x_k) \) with corresponding price vectors \( p_a \) and \( p_b \). We then have the following definition.

**DEFINITION: WEAK SEPARABILITY.** A utility function \( u(x) \) is weakly separable in the \( b \)-goods if there exists a subutility function \( v(b) \) and a macro function \( u'(a, v(b)) \), which is continuous and monotonically strictly increasing in \( v(b) \), such that \( u(a,b) = u'(a, v(b)) \).

The subutility function \( v \) is a utility function in its own right with the usual properties. Weak separability of \( u \) in the \( b \) goods means that the marginal rate of substitution between any two elements of the \( b \) vector is independent of all elements of the \( a \) vector. Note that the utility function can be separable in \( b \) but not in \( a \).\(^4\)

When the utility function \( u \) is separable in \( b \), its value does not depend on the elements of \( b \) individually but rather on their combined subutility value \( v(b) \). The household in effect solves its budgeting decision in two stages: first divide expenditures between \( a \) and \( b \), and then decide the optimal allocation among the elements of \( b \) independently of the choices of the elements of \( a \) (Gorman, 1959). When utility is separable, the econometrician can confine analysis to the \( b \) elements and simply disregard the \( a \) goods (except in specifying the relevant budget constraint). In particular, if the utility function is separable in nondurables and services, one can ignore the service flow of durables in studying the household's choice between nondurables and services, greatly simplifying the analysis.\(^5\)

Varian (1982, 1983) provides two tests of separability. The first test is the weaker of the two, checking if necessary consistency conditions are met. The subdata \( b \) must satisfy GARP because each observation on \( b \) must solve the problem

\(^4\)See Blackorby, Primont, and Russell (1978) for more discussion of separability.

\(^5\) Use of this simplifying procedure is routine in both Euler equation and consumption function studies. For example, Hall (1978) uses nondurables plus services, and Flavin (1981) uses nondurables alone.
\[
\max v(b)
\]
subject to \( p_b b \leq p_m b \)

So it is necessary for separability that Afriat numbers exist for the \( b \) subdata, because otherwise the \( v \) subutility function does not exist. A test of necessary conditions therefore can be done by checking if the subdata \( b \) satisfy GARP.

The second test is stronger because it checks necessary and sufficient conditions for separability. For sufficiency, the Afriat numbers for the subutility function \( v \) must be consistent with those for the utility function \( u \).

The following theorem from Varian (1983) states the relationship precisely:

**VARIAN'S THEOREM.** The following conditions are equivalent.

(i) There exist numbers \( U_t, V_t, \lambda_t, \mu_t > 0 \), that satisfy the Afriat inequalities

\[
U_t \leq U_s + \lambda_t p_m(a_t - a_s) + (\lambda_t/\mu_t)(V_t - V_s)
\]

\[
V_t \leq V_s + \mu_t p_m(b_t - b_s)
\]

for \( s, t = 1, \ldots, T \).

(ii) The data \((p_{bt}, b_t)\) and \((p_{at}, 1/\mu_t; a_t, V_t)\) satisfy GARP for some choice of \((V_t, \mu_t)\) that satisfies the Afriat inequalities.

(iii) There exists a weakly separable nonsatiated, continuous, concave, monotonic utility function that rationalizes the data.

Part (i) provides the means for testing the necessary and sufficient conditions; one must construct two sets of interrelated Afriat numbers. Varian has written a computer routine to do the calculations. However, Varian's program actually performs only a sufficient test for weak separability because of computational constraints; see Swofford and Whitney (1994). Therefore, if the data pass the necessary conditions in the first test but fail the sufficient conditions in the second test, we cannot rule out the possibility that the separability assumption in question in fact does hold. Of course, if the necessary condition fails or the sufficient condition passes, then the results of the tests are definite.

3. **Test Implementation and Properties.** The GARP and Separability tests are done with Varian's NONPAR software, which he kindly provided. NONPAR does the linear programming exercise necessary to see if the data satisfy GARP and reports any violations. A violation occurs when a consumption bundle is revealed not preferred

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6Swofford and Whitney (1994) develop a test of the necessary and sufficient conditions in Varian's theorem. Unfortunately, it is computationally very intensive and cannot be performed for samples of the sizes in our paper; see Swofford and Whitney (1994) for further discussion.
in one period but then is bought in another period even though the bundle previously revealed preferred is a feasible choice.

The NONPAR tests have both advantages and disadvantages. The main advantage is that the tests are non-parametric; one need not specify the form of the utility function. Also, the tests can handle a large number of goods. The main disadvantage is that the tests are non-stochastic. Violations are all or nothing; either there is a utility function that rationalizes the data or there is not. We therefore must be especially careful about the possibility of measurement error. If there were no measurement error, then any observed rejection of GARP would be a genuine rejection. However, with measurement error, false rejections may occur, and without a distribution theory for the tests, we cannot judge the importance of observed rejections by the conventional significance tests.\textsuperscript{7} We respond to this difficulty by faithfully reporting all rejections and by adding some judgmental discussion of the likely significance of the test results. The reader should bear in mind, though, that there is a bias toward rejection (Barnett and Choi, 1989) because even one inconsistency leads to total rejection of GARP; consequently, passing the GARP tests is a very strong result.

Despite their problems, the GARP tests provide useful information. It is true that one must exercise caution in interpreting the tests because of their non-stochastic nature. However, the only available alternative is to do no testing and simply proceed with inference conditional on untested assumptions about the existence of a representative agent and the separability properties of his utility function. We believe it preferable to use the GARP tests, particularly in view of the results we report below.

3. DATA AND THE USER COST OF DURABLE GOODS

Our goal is to see if there is a utility function consistent with the U.S. aggregate consumption data and if it is separable in any of its arguments. To do this, we perform Varian's tests on monthly, quarterly, and annual data

\textsuperscript{7}Varian (1985) and Epstein and Yatchew (1985) have extended Varian's (1982,1983) test to a stochastic environment by allowing for the presence of measurement error. Their implementation requires certain assumptions about the measurement error process including knowledge of its variance and so we do not pursue these tests here. Bronars (1987) reports simulation evidence on the rejection frequencies of Varian's GARP test when the consumption data are random. His design assumes nine categories of consumption goods and 31 years of annual data. His results indicate the power is in excess of 0.91 against this alternative when per capita consumption data are used.
for the United States spanning the periods 1959:01-1990:12, 1959.1-1990.4 and 1929-1990, respectively. All data are described in Appendix 2. We assume the service flows from durables are proportional to the durable stocks, so the flows can be measured by the stocks, as in Deaton and Muellbauer (1980).8

The tests require a price for each good. Prices for nondurables and services are readily available in the official statistics, but proper prices for durables are not. We need the user cost of durables, but official statistics report only the sale prices for new durables. We therefore construct measures of the user cost, and we describe how we did so in the remainder of this section.9

The formula for the user cost of durable good i in period t is

\[ \hat{p}_{rel,t}^{uc} = p_{rel,t}^d - (1-\delta_t)E_t(m_{t,t+1}p_{rel,t+1}^d) \]

where \( p_{rel,t}^{uc} \) is the user cost relative to some nondurable numeraire, \( p_{rel,t}^d \) is the relative price of a unit of the durable, \( \delta \) is the depreciation rate, \( m_{t,t+1} \) is the intertemporal marginal rate of substitution for the numeraire consumption good, and \( E_tX_{t+1} \) denotes the conditional expectation at time t of X at time t+1. The usual practice is to assume \( \delta \) is the same for all goods.10 We do not follow that practice but instead use different depreciation rates for each of the eleven categories of durables. Depreciation rates differ substantially across types of goods, so it seems prudent not to impose one average rate on everything.

We must adjust (3) in two ways to use it in constructing the user costs that we need for our tests. First, we cannot observe \( m_{t,t+1} \), which depends on the particulars of the utility function. We therefore approximate it by \( (1+r_t)^{-1} \), where r is the real interest rate. We thus have

\[ \hat{p}_{rel,t}^{uc} = p_{rel,t}^d - (1-\delta_t)(1+r_t)^{-1}E_t(p_{rel,t+1}^d) \]

This approximation makes no "risk correction" and thus ignores the effect of uncertainty on the value of assets.

Second, the foregoing equation is in terms of relative prices, whereas we need prices in money terms for the GARP tests (because we must multiply each quantity by its price in checking for violations of the GARP conditions). We

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8We ignore the possibility that both non-durables and services as measured by the National Income Accounts contain durable elements. See Fleissig (1993) and the references provided there for treatments of that issue.

9The use of user costs is one of the features that distinguishes our work from that of Manser and McDonald (1988), who use the price of new durables rather than the user cost.

10For example, Diewert (1974) and Swofford and Whitney (1987, 1988) set \( \delta \) at 0.10 for all goods, and Christensen and Jorgenson (1969) set it at 0.20.
therefore replace all prices in the right side with their nominal equivalents - that is, money prices $p^d$ replace $p^d_{rel}$
and the nominal interest rate $R$ replaces the real rate $r$. We have finally

\begin{equation}
    p^u_w = p^d_w - (1-b)(1+R)^{-T}E_t(p^d_{t+1})
\end{equation}

Next, we face the problem of measuring expected prices because the right side of (4) contains the expected durables
price $E_{it+1}p^d_{it+1}$. Previous work, such as Diewert (1974) and Swafford and Whitney (1987, 1988), has used static
expectations, according to which the expected price for next period is simply the current period’s actual price:

$$E_{t}p^d_{t+1} = p^d_{t}$$

This scheme implies that people think $p^d$ is a driftless random walk and so do not adjust the current price in
predicting next period’s price. Inflation implicitly is regarded as white noise, and its expected value always is zero.

Such rigid expectations seem implausible, especially because $p^d$ in fact is not a driftless random walk and inflation
is not white noise. However, we use the static scheme as one of our models of expectations formation both because
it has been used by others and because it provides a kind of lower bound on expectations behavior. At the other
extreme is the perfect foresight model, according to which people know next period’s price exactly:

$$E_{t}p^d_{t+1} = p^d_{t+1}$$

Perfect foresight, too, seems implausible, and in addition it yields a few observations of negative user costs that
required somewhat arbitrary adjustments to correct, described momentarily.\footnote{Negative user costs have the implausible implication that the good is more than free: its use pays rather than costs
the user.} Nonetheless, because of its simplicity, we use it to construct an alternate user cost series.

Given the limitations of both static expectations and perfect foresight, we also estimated ARIMA models
for the various $p^d_e$ and took expectations of them. We fitted several models to each of the individual durables series
but the resulting user costs yielded test results much like those from the perfect foresight model and provided no
additional insights. We therefore do not report any results based on the ARIMA models to save space.

The annual data include the Second World War, which created a special problem with perfect foresight.
Under perfect foresight, the user costs for autos, other autos, furniture, kitchen appliances, other household
appliances, video and audio and ophthalmic products are negative for some war years 1941-1946. In those years
there were restrictions on new investment, and repairs sometimes could not be made because of parts and labor shortages. Consequently, there were increases in depreciation and discards not captured by our depreciation rate measures, which are constant for all years. To adjust for these war year factors, we interpolated between the 1940 and 1947 user cost levels by repeatedly increasing the depreciation rate for each good by 0.05% per iteration until the user cost was within 15% of the 1940 and 1947 levels respectively.

4. TEST RESULTS

We now report the results of applying Varian's GARP and Separability tests to this data set on aggregate consumption for the U.S..

1. GARP Tests. Under the static expectations model, the annual data pass GARP, but the quarterly and monthly data both fail. Under both perfect foresight, all three data sets fail. Table 1 reports the numbers of violations.

Previous tests of GARP in the literature have focused exclusively on the number of violations. However it is also of interest to know when these violations occur because then we can define subsamples over which GARP is satisfied. We used the following method, apparently original to this paper, to identify these "breakpoints." First, we applied the GARP tests to the whole sample. The tests compare every year's consumption bundle and prices to every other year's bundle and prices and report any violations of GARP. For example, if observations 25 and 35 are inconsistent with each other, the tests report violations for observations 25-35 and 35-25. We then split the sample at these points and re-ran the GARP tests within the resulting subsamples. Working through the violation list this way allowed us to construct the largest possible subsamples consistent with GARP and identify the periods where there is a break in consistency. Table 2 reports the resulting GARP-consistent subsamples.

With static expectations, the annual data pass GARP over the full sample, the quarterly data pass over the subsample 1960.1-1991.4, and the monthly data have no subsample of any appreciable length that passes. With perfect foresight, the annual data pass GARP over the two subsamples 1935-1981 and 1982-1990, the quarterly data pass over the two subsamples 1960.1-1980.4 and 1981.4-1991.4 (notice the discontinuity), and the monthly data pass over the subsamples 1960.01-1968.07, 1968.08-1970.05, and 1970.06-1993.05. Clearly, the results are sensitive to the method of expectation formation. There are several other noteworthy aspects of these results.
First, for the quarterly and monthly data, the full samples are inconsistent with the decisions of a representative agent whose utility function is intertemporally separable, irrespective of the expectations scheme assumed. For the annual data, the results on the full sample are mixed, accepting consistency with GARP under one expectations scheme but rejecting it under the other. For the most part, then, the data seem inconsistent with a representative agent maximizing an unchanging, intertemporally separable utility function over the full sample periods. The data, however, could be consistent with this type of representative agent model if the parameters or the functional form of the utility function changed appropriately at the breakpoints indicated above. Interestingly, the annual and quarterly data with perfect foresight nearly agree on whether and when a break occurs. Under static expectations, the annual and quarterly samples are continuous over 1960-1990, whereas under perfect foresight they both show a break in 1981. The 1981 break is especially strong in the quarterly data, which show a discontinuity between the 1980.4 and 1981.4 observations and which violate GARP for every possible pairing within the discontinuity period. The strength of the quarterly results and their consistency with the annual results suggests something more than just an artifact of measurement error. Also, this pattern of rejections is consistent with preferences being constant over the four quarters of the year for years on either side of the 1980-81 period. Previous studies (e.g., Browning, 1989), hypothesized that GARP would fail in quarterly data because preferences might be periodic over the quarters, but the data do not support that hypothesis. The monthly data do not show breaks at the same points as the annual and quarterly data, but there is some reason to believe the monthly data simply are inadequate, as has been noted in the literature (Wilcox, 1992) and as we discuss in more detail below.

Second, we never find a break in 1979 for the annual or quarterly data. The supposed change in Federal Reserve operating procedure that year is often cited as a possible source of instability in consumption-based asset pricing models (e.g., Ghysels and Hall, 1990). Our results suggest there is no problem with 1979 for consumption analysis, although there are problems with other years.

Third, the results suggest special problems with the monthly data. Under static expectations, there is no

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12 This conclusion differs from that of Manser and McDonald (1988), who fail to reject GARP for annual data (the only data they test). Our tests show that whether or not the annual data are consistent with GARP depends on the expectations scheme, which affects the user cost of durables. Manser and McDonald use new durables’ prices rather than user costs as the price of durables and so never address the expectations problem. However our results agree with those of Browning (1989), who reported that the annual data for 1954-79 satisfy GARP.
GARP-consistent subsample long enough to use in an econometric study. The results for perfect foresight are much less drastic, but even there the longest period is only 24 years long. For "short-run" kinds of questions, 24 years (or 288 months) may be a sufficiently long sample, but they are unlikely to be adequate for "long-run" issues where the span of the data is more important than the frequency of observation. We discuss the monthly data further in the next section.

Finally, there is no systematic relation between the expectation schemes and the test results. For monthly data, perfect foresight gives fewer rejections than static expectations, but the opposite is true for the annual and quarterly data.

2. Separability Tests. The separability tests are an extension of the GARP tests (see Varian's Theorem above) and so can be done only on data consistent with GARP. We therefore restrict attention to the sample periods listed in Table 2.

We examine the separability assumptions most frequently used in the consumption literature. Our annual data set reports expenditure on 62 categories of consumption goods - 17 types of nondurables, 34 types of services, and 11 types of durables; the quarterly and monthly data have fewer series (see Appendix 2, part c). In conducting our tests, we construct subsets ("groups") of these categories but at no time do we aggregate them, thus avoiding any possible problems associated with a particular method of aggregation.\textsuperscript{13} We perform our tests under both static expectations and perfect foresight. The results are reported in Table 3.

The annual and quarterly data tell the same story, without much difference between the two expectations schemes. The first hypothesis, S1, is that the three major categories of consumption expenditure are mutually separable from each other. That hypothesis does not pass either the necessary or the necessary and sufficient conditions, implying that at least one of the categories of expenditure cannot be analyzed independently of the other two.

The next three hypotheses examine the possibility that durables are separable from nondurables and

\textsuperscript{13}In contrast, Swofford and Whitney (1987, 1988) use only the aggregate totals for nondurables, services, and durables reported in the NIPA data. Those aggregates presuppose an amount of separability not consistent with the data, as we show below. They also are created by the simple-sum method, which seems inappropriate in light of our separability results.
services. The upshot is that they are not. Hypothesis S2 proposes mutual separability of nondurables and services as a group on the one hand and durables on the other. S3 is the same as S2 except that clothing and shoes are reclassified as durables rather than nondurables as suggested by Darby (1974), and S4 weakens S2 to one-sided separability of durables from the group of nondurables and services. None of the three passes the necessary and sufficient conditions; only S3 passes the necessary conditions and then only for annual data under perfect foresight.

The remaining hypotheses examine if nondurables alone or nondurables and services together are separable from durables. The first three of these hypotheses - S5, S6, and S7 - give inconclusive results, usually passing the necessary conditions but failing the necessary and sufficient conditions. These results looked promising, so we explored further by ungrouping the durables category into its components. Space prohibits reporting all the combinations we tried, so we report the successes and some close relatives. Note that in Table 3 the first seven separability tests S1-S7 are the same for all frequencies of data. For the annual data, hypothesis S8 passed the necessary and sufficient conditions for both expectations schemes. That hypothesis splits durables into motor vehicles, other autos, and all remaining durables. These three subcategories and the group of nondurables and services are all mutually separable. Hypothesis S9 is but one example showing that even a slight attempt to consolidate these categories leads to much weaker test results. Hypothesis S10 tries to separate nondurables and services, given the durables divisions of S8, but is rejected. For the quarterly data, hypotheses S11 and S12 both fail all tests, but the closely related hypothesis S13 passes the necessary and sufficient conditions for both expectations schemes. Hypothesis S12 shows that a slight reformulation of S13 leads to rejection.

The main implication of these results is that for annual or quarterly data an econometric analysis of nondurables and services as a group, paying no attention to durables, is valid but analysis of either nondurables alone or durables alone is not. Also, when analyzing all three categories at once, one must divide durables into the subcategories shown in hypotheses S8 and S13. It is of interest to compare our results with Wilcox's (1992) recommendations based on an analysis of the measurement system for consumption data. His analysis suggested that one may wish to disaggregate consumption expenditure into (at least) three groups: motor vehicles, services, and the rest. Our results provide empirical support for the treatment of motor vehicles as a separate group, but reject the treatment of services as a separate group.
Finally, let us return to the results for the monthly data. None of the separability hypotheses pass the necessary and sufficient conditions; only one hypothesis passes the necessary conditions, and even then not over all sample periods. These results are in striking contrast to those for the annual and quarterly data, and there are at least two ways to interpret them. The first interpretation accepts the results at face value, in which case analysis of monthly data cannot ignore any category of consumption expenditure in examining the behavior of any other category. The second interpretation is that the results are artifacts of bad data. Recall that it is difficult to find subsamples of the monthly data that pass GARP. Perhaps those difficulties and the monthly data's different separability implications both reflect the problems reported by Wilcox (1992) with the methods used to construct the monthly data. If so, the monthly data may be of questionable value for analyzing consumption based on the representative agent model.

5. CONCLUDING REMARKS

In this paper we have used Varian's (1982, 1983) non-parametric tests to examine two issues pertaining to the representative agent model. First, we use the GARP tests to investigate whether aggregate consumption data for the U.S. could have been generated by a representative agent whose utility function is intertemporally separable. Second, we explore the separability structure of the representative agent's utility function. Although the non-parametric tests have some limitations, the alternative of not testing at all obviously also has some shortcomings.

The GARP tests almost uniformly find that the data are inconsistent with a representative agent model with intertemporally separable utility over the full period of available data. The exception is annual data under static expectations. Annual data under perfect foresight and quarterly data under either scheme all show a break in behavior around 1981, which suggest that the representative agent model with intertemporally separable utility either is wrong altogether or at least that the utility function changed after 1981. Finally, the monthly data exhibit so many violations of GARP that they cannot be consistent with an intertemporally additive utility function that is constant for any appreciable length of time.

Many empirical studies of consumption based on this type of representative agent model use samples over
which our tests reject GARP. One interpretation of our results is that those studies use misspecified models. However, such a conclusion may be premature. Because a rejection with the GARP test is all or nothing, we cannot assess whether the violations are more likely to be due to measurement error or some more fundamental change in the model, nor can we assess the likely impact of violations of GARP on the estimation of the parameters of Euler equations derived from the representative agent model. All of these issues are important areas for future research. Until such work becomes available, however, we believe our results may be best regarded as a non-parametric structural stability test that suggests caution in estimating and interpreting any representative agent model estimated with annual or quarterly data that include observations for 1981 or estimated with any set of monthly data at all.

An alternative explanation for our results is that the representative agent has preferences that vary seasonally (thus causing the large number of GARP rejections in the monthly data) or has a utility function is not intertemporally separable. An associate editor has pointed out that testing for seasonality in the monthly data could be done by creating twelve data sets, one comprising all the January observations, another comprising all the February observations, and so on, and then testing each of the twelve data sets for consistency with GARP. GARP consistency of the twelve separate data sets would be strong evidence that the rejections in the total data set were the result of seasonally varying preferences. This extensive testing would be an interesting topic for future research. With respect to intertemporal separability, it is entirely possible that the data are consistent with a structurally constant utility function possessing such features as habit persistence. That is a plausible explanation for the high number of violations of GARP with the monthly data, although there are other grounds for suspecting the monthly data are just of poor quality (Wilcox, 1992). However, it then is very striking that we found so few violations of GARP with the quarterly and annual data, suggesting that any habit formation effects persist for less than three months.

Let us turn now to the separability tests. These tests can be applied only to data sets that pass GARP, so for the rest of this discussion we focus exclusively on those subsets of the annual and quarterly data consistent with GARP. The results show that the main categories of consumption (nondurables, services, and durables) are not mutually separable, so one should not analyze arbitrary subsets of the consumption data. However, nondurables
and services are separable from durables, although not vice versa. This result implies that nondurables and services can be analyzed together as a group independently of durables, but not vice versa. Also, we find evidence that motor vehicles should be treated as a separate group.

Most studies use a single aggregate of nondurable and services expenditures as their measure of consumption and ignore durables. According to our separability results, that procedure is legitimate for annual and quarterly data. If one wants to include durables, however, our separability tests reject forming a single aggregate of durable goods. Rather, one should divide durables into some combination of motor vehicles, other autos, furniture, and other durables, the exact combination depending on whether the data are quarterly or annual.
### TABLE 1
GARP Test Results

<table>
<thead>
<tr>
<th>Data Frequency</th>
<th>Monthly</th>
<th>Quarterly</th>
<th>Annual</th>
</tr>
</thead>
<tbody>
<tr>
<td>Model</td>
<td>221</td>
<td>43</td>
<td>0</td>
</tr>
<tr>
<td>Static</td>
<td>157</td>
<td>55</td>
<td>11</td>
</tr>
</tbody>
</table>

### TABLE 2
GARP-Consistent Subsample Periods

<table>
<thead>
<tr>
<th>Data Frequency</th>
<th>Monthly</th>
<th>Quarterly</th>
<th>Annual</th>
</tr>
</thead>
<tbody>
<tr>
<td>Model</td>
<td>1974.10-1978.11</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Perfect</td>
<td>1970.05-1990.12</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>
### TABLE 3
Tests for Weak Separability

<table>
<thead>
<tr>
<th>Separability Hypothesis</th>
<th>Expectations Model</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Static Expectations</td>
</tr>
</tbody>
</table>

#### Annual Data

- S1: $f[u_1(nond), u_2(ser), u_3(dur)]$
- S2: $f[u_1(nond, ser), u_4(dur)]$
- S3: $f[u_1(nond-clothing, ser), u_3(dur, clothing)]$
- S4: $f[nond, ser, u_1(dur)]$

<table>
<thead>
<tr>
<th></th>
<th>Static</th>
<th>Perfect</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td>Foresight</td>
</tr>
<tr>
<td>S5: $f[u_1(nond, ser), dur]$</td>
<td>N&amp;S</td>
<td>N</td>
</tr>
<tr>
<td>S6: $f[u_1(nond), u_2(ser, dur)]$</td>
<td>N&amp;S</td>
<td>X</td>
</tr>
<tr>
<td>S7: $f[u_1(nond), ser, dur]$</td>
<td>N</td>
<td>N</td>
</tr>
<tr>
<td>S8: $f[u_1(nond, ser), u_4(motor vehicles), u_3(other autos), u_5(remaining nine durables)]$</td>
<td>N&amp;S</td>
<td>N&amp;S</td>
</tr>
<tr>
<td>S9: $f[u_1(nond, ser), u_5(motor vehicles, other autos), u_4(remaining nine durables)]$</td>
<td>N</td>
<td>X</td>
</tr>
<tr>
<td>S10: $f[u_1(nond), u_2(ser), u_3(motor vehicles), u_4(other autos), u_5(remaining nine durables)]$</td>
<td>X</td>
<td>X</td>
</tr>
</tbody>
</table>

#### Quarterly Data

- S1: $f[u_1(nond), u_2(ser), u_3(dur)]$
- S2: $f[u_1(nond, ser), u_4(dur)]$
- S3: $f[u_1(nond-clothing, ser), u_3(dur, clothing)]$
- S4: $f[nond, ser, u_1(dur)]$

<table>
<thead>
<tr>
<th></th>
<th>Static</th>
<th>Perfect</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td>Foresight</td>
</tr>
<tr>
<td>S5: $f[u_1(nond, ser), dur]$</td>
<td>N</td>
<td>N</td>
</tr>
<tr>
<td>S6: $f[u_1(nond), u_2(ser, dur)]$</td>
<td>N</td>
<td>N</td>
</tr>
<tr>
<td>S7: $f[u_1(nond), ser, dur]$</td>
<td>N</td>
<td>N</td>
</tr>
<tr>
<td>S11: $f[u_1(nond), u_2(ser), u_3(motor vehicles), u_4(furniture, other durables)]$</td>
<td>X</td>
<td>X</td>
</tr>
<tr>
<td>S12: $f[u_1(nond, ser), u_5(motor vehicles, furniture), u_4(other dur)]$</td>
<td>X</td>
<td>X</td>
</tr>
<tr>
<td>S13: $f[u_1(nond, ser), u_5(motor vehicles), u_3(furniture, other dur)]$</td>
<td>N&amp;S</td>
<td>N&amp;S</td>
</tr>
</tbody>
</table>

(Table continues on next page)

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See notes at the end of Table.
TABLE 3 (Continued)
Tests for Weak Separability

<table>
<thead>
<tr>
<th>Separability Hypothesis</th>
<th>Expectations Model</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Static Expectations</td>
</tr>
<tr>
<td></td>
<td>Monthly Data</td>
</tr>
<tr>
<td></td>
<td></td>
</tr>
<tr>
<td>S1: ( f[u_1(\text{nond}),u_2(\text{ser}),u_3(\text{dur})] )</td>
<td>X</td>
</tr>
<tr>
<td>S2: ( f[u_1(\text{nond},\text{ser}),u_4(\text{dur})] )</td>
<td>X</td>
</tr>
<tr>
<td>S3: ( f[u_1(\text{nond-clothing,ser}),u_3(\text{dur,clothing})] )</td>
<td>X</td>
</tr>
<tr>
<td>S4: ( f[\text{nond,ser},u_1(\text{dur})] )</td>
<td>X</td>
</tr>
<tr>
<td>S5: ( f[u_1(\text{nond,ser}),\text{dur}] )</td>
<td>X</td>
</tr>
<tr>
<td>S6: ( f[u_1(\text{nond}),u_2(\text{ser,dur})] )</td>
<td>X</td>
</tr>
<tr>
<td>S7: ( f[u_1(\text{nond}),\text{ser,\text{dur}}] )</td>
<td>X</td>
</tr>
<tr>
<td>S11: ( f[u_1(\text{nond}),u_2(\text{ser}),u_3(\text{motor vehicles,\text{fur}}) )</td>
<td></td>
</tr>
<tr>
<td>( u_3(\text{furniture,other durables}) )</td>
<td>X</td>
</tr>
<tr>
<td>S12: ( f[u_1(\text{nond,ser}),u_3(\text{motor vehicles,furniture,\text{fur}}) )</td>
<td></td>
</tr>
<tr>
<td>( u_3(\text{other dur}) )</td>
<td>X</td>
</tr>
<tr>
<td>S13: ( f[u_1(\text{nond,ser}),u_2(\text{motor vehicles,\text{fur}}) )</td>
<td></td>
</tr>
<tr>
<td>( u_3(\text{furniture,other dur}) )</td>
<td>N*</td>
</tr>
</tbody>
</table>

NOTE:

Annual Data
dur, nond, ser = \{11 durable goods\}, \{17 nondurable goods\},
\{34 services\}

N: passes necessary condition
N&S: passes necessary condition and a sufficient condition
X: fails all conditions

Test results apply to all subsample periods except when marked by an asterisk (*), in which case the separability test FAILED for the sample period 1990.07-1990.12.
APPENDIX 1. SARP AND GARP

DEFINITIONS.

(1) \( x_i \) is directly revealed preferred to \( x \), written \( x_i R^0 x \), if \( p_i x_i \geq p_x x \).

(2) \( x_i \) is strictly directly revealed preferred to \( x \), written \( x_i P^0 x \), if \( p_i x_i > p_x x \).

(3) \( x_i \) is revealed preferred to \( x \), written \( x_i R x \), if \( p_i x_i \geq p_j x_j , p_j x_j \geq p_k x_k ,..., p_m x_m \geq p_n x_n \) for some sequence of observations \( \{x_i, x_j, ..., x_m\} \).

(4) \( x_i \) is strictly revealed preferred to \( x \), written \( x_i P x \), if there exist observations \( x_j \) and \( x_k \) such that \( x_i R x_j \), \( x_j P x_k \), \( x_k R x \).

AXIOMS.

(1) SARP. The following statements of SARP are equivalent.

(A) \( x_i R x_j \) and \( x_j R x_i \Rightarrow x_i = x_j \)

(B) \( x_i R x_j \) and \( x_i \neq x_j \Rightarrow \) not \( x_j R x_i \)

(C) \( x_i R x_j \) and \( x_i \neq x_j \Rightarrow \) not \( x_j R^0 x_i \)

(2) GARP.

\( x_i R x_j \Rightarrow \) not \( x_j P^0 x_i \)

APPENDIX 2

PART A: ANNUAL DATA

Population. All stocks and flows are measured in per capita terms. Population is measured as Total Population from the Report of the Council of Economic Advisors, various issues.

Consumption expenditure. For 1929-1982, quantities and prices are from the National Income and Product Accounts, U.S. Personal Consumption Expenditures, Tables 2.6 and 2.7. For 1983-1990, the data are from the Bureau of Economic Analysis tapes. Quantities are real 1987 dollars, and prices are normalized to a base.
of 1987=100. The earlier data are reported in 66 categories of consumption expenditure. The later data are divided into more detailed categories than that, so we aggregated them up to the earlier categories. Our analysis uses all 17 categories of nondurable expenditure and 34 of the 36 categories of service expenditure, omitting net foreign remittances and net foreign travel which sometimes are negative and so unusable. The latter two series together always amount to less than 1% of total consumption expenditure.

Although the NIPA data report 13 types of durable goods expenditure, the Survey of Current Business reports only 11 stock series. We therefore aggregated up the relevant categories in the NIPA data to match those of the SCB.

Depreciation rates. The following service lives, in years, are from the Fixed and Reproducible Tangible Wealth: autos (10), other motor vehicles (8), furniture (14), kitchen and other household appliances (11), china (10), other durable households (10), radio and musical instruments (9), jewelry (11), ophthalmic products and orthopedic appliances (6), books (10) and wheel goods (10). We use the reciprocal of a durable's expected number of service years as the depreciation rate for that good.

Interest rate. The interest rate is the 6-month prime commercial paper rate, taken from the Survey of Current Business. We use this rate because it is the closest series to a 1 year rate dating back to 1929.

PART B: QUARTERLY DATA

Consumption expenditure. Data are from the National Income and Product Accounts, Private Consumption Expenditure, Seasonally Adjusted Quarterly Totals at Annual Rates, 1959.1 - 1990.4 Constant Cost (Billions of 1987 dollars). The quarterly NIPA data have only 14 disaggregated series.

We calculate the quarterly stocks of consumer durables from the annual data as in Campbell and Mankiw (1990) because there are no quarterly data available. We measure the quarterly stock of durable goods as the average of the end-of-quarter stock and previous end-of-quarter stock. We use the annual stock for 1958 as the end-of-quarter stock for the initial quarter 1959.1. We then construct the end-of-quarter stocks in the usual way by depreciating the previous quarter's stock and adding the current quarter's expenditure on the durable in question. We calculate the depreciation rate \( \delta \), from \( k_t = d_t - (1-\delta)k_{t-1} \), by selecting a depreciation rate for each category until the
stock in 1990.4 is close to the annual stock for 1990. The depreciation rates (in percent) per quarter are: total durables (6), (the same rate as Campbell and Mankiw, 1990), motor vehicles and parts (5.9), furniture and household equipment (4.2) and other durables (4.6). These depreciation rates may seem high, but note that they ignore discards. Annual stock measures are net of discards, so their depreciation rates are necessarily lower than those for the gross quarterly stocks.

Interest rate. The interest rate is from J. Huston McCulloch and Heon-Chul Kwon, Ohio State University Working Paper # 93-6, series ZEROYLD1. This monthly interest rate has three months to maturity and is aggregated over (Dec,Jan,Feb), (Mar,Apr,May), (June,July,Aug), (Sep,Oct,Nov) into a quarterly series. (This interest rate is not used for the annual data because it does not date back to 1929.)

PART C: MONTHLY DATA

The monthly data set is created using the same technique as in the quarterly data set. The PCE monthly series are from Citibank Database for 1959:01-1990:12. The following series are used.

GMCDAQ - motor vehicles and parts
GMCDQF - furniture and household equipment
GMCDOQ - other durables

GMCNCQ - clothes and shoes
GMCNFQ - food
GMCNGQ - gasoline and oil
GMCNOQ - other nondurable goods
GMCNOFQ - fuel, oil, and coal

GMCSHQ - housing services
GMCSGQ - housing operations
GMCSMQ - medical care services
GMCSOQ - other services
GMCSSTQ - transportation services

P16 - total civilian population
INT - interest rate is from Thornton and Yue (1992) and is the highest rate that the agent can obtain in financial markets.
REFERENCES


