Applied Geoscience Data Analysis using Matlab

07 Nov 2013

(Lecture 20)

Referencing Matrix, Profiling & Terrain Analysis

Referencing Vector (from last lecture)

R = [cells/angular unit, north-latitude, west-longitude]

Where north-latitude and west-longitude refer to the edges of the upper-left corner.

Requires equal x-y spacing!

Example from last lecture

For ETOPO2 (2 minute or 2/60 = 1/30 degree spacing)  
(i.e., a dataset with \( \frac{1}{2} \) the resolution of ETOPO1)

\[ R = [30, 20+1/60, 30-1/60]; \]

Limits of the node registered file, plus \( \frac{1}{2} \) grid space to the north and west of north-west most node.

\[ R = 30.0 \quad 20.0167 \quad 29.9833 \]

Referencing Matrix (R)
- new/expanded in version 3.0 of the mapping toolbox
- Allows for a different spacing in the x and y dimensions of the grid

R is a 3-by-2 matrix that transforms pixel subscripts (row, column) to map coordinates \( (x, y) \) according to:

\[ [x \ y] = [\text{row col 1}] \ast R \]

Or transforms pixel subscripts to/from geographic coordinates according to

\[ [\text{lon lat}] = [\text{row col 1}] \ast R. \]
R = makerefmat(X_{11}, Y_{11}, DX, DY)
- DX and DY are scalars giving the spacing between pixels.
X_{11} and Y_{11} are scalars that specify the location of the center of the first (1,1) entry in the NODE registered sense.

DX is the difference in X (or longitude) between pixels in successive columns
DY is the difference in Y (or latitude) between pixels in successive rows.

R = 
\[
\begin{bmatrix}
0 & -0.01667 & 29.9833 \\
0.01667 & 0 & 20.01666 \\
29.9833 & 20.01666 & 0
\end{bmatrix}
\]

\[\text{[lon lat]} = \text{[row col 1]} \times R.\]
\[[1 1 1]^T R = 30 20\]

Referencing Matrix (example for ETOPO2 dataset)
R = makerefmat(X_{11}, Y_{11}, DX, DY)
R = makerefmat(30,20,1/60,-1/60)  % note the negative DY

R = 
\[
\begin{bmatrix}
0 & -0.01667 & 29.9833 \\
0.01667 & 0 & 20.01666 \\
29.9833 & 20.01666 & 0
\end{bmatrix}
\]

Extracting values z from the geo-referenced gridded data
VAL = itln2val(Z, R, LAT, LON) interpolates a regular data grid Z with referencing vector R at the points specified by vectors of latitude and longitude, LAT and LON. R is either a 1-by-3 vector containing elements:

\{cells/degree northern_latitude_limit western_longitude_limit\}
or a 3-by-2 referencing matrix that transforms raster row and column indices to/from geographic coordinates according to:

\[\text{[lon lat]} = \text{[row col 1]} \times R.\]
If R is a referencing matrix.
Profiling: 1st define points to sample

`TRACK2` Geographic tracks from starting and ending points

```matlab
[lat,lon] = TRACK2(lat1, lon1, lat2, lon2) computes great circle tracks on a sphere starting at the point lat1, lon1 and ending at lat2, lon2. The inputs can be scalar or column vectors.

[tr_lat, tr_lon] = track2(0,10,0,16,30,60)
```

Also See

track1 trackg

Then extract the values at these points

```matlab
trz = ltn2val(ETOPO1,R,tr_lat, tr_lon);
trd = distance(tr_lat, tr_lon);
figure; plot(deg2km(trd),trz); grid on
xlabel('distance km'); ylabel('elevation m');
```

An alternative to ltn2val.

```matlab
[zi,rng] = mapprofile(Z,R,lat,lon) accepts as input a regular data grid and waypoint vectors. No displayed grid is required. Sets of waypoints may be separated by NaNs into line sequences. The output ranges are measured from the first waypoint within a sequence. R is either a 1-by-3 vector containing elements:

[cells/degree northern_latitude_limit western_longitude_limit]
```

or a 3-by-2 referencing matrix that transforms raster row and column indices to/from geographic coordinates according to:

```matlab
[lon lat] = [row col 1] * R.
```

If R is a referencing matrix,

Many of the mapping toolbox function default to a spherical earth model; however, you can also specify the reference ellipsoid.

For example,

```matlab
[zi,rng] = mapprofile(Z,R,lat,lon,ellipsoid)
```

Or

```matlab
[arclen,az] = distance(lat1,lon1,lat2,lon2,ellipsoid)
```

- Where ellipsoid is a vector of the form:
  ```matlab
  [semimajor_axis, eccentricity]
  ```

- The output, arclen, is expressed in the same length units as the semimajor axis of the ellipsoid.
Sample Ellipses with Various Eccentricities
(focal points are marked; the diagrams are only approximately to scale)

Circle with b/a=1;  e = 0

Ellipse with b/a=3/5;  \( e = \sqrt{1-9/25} = 4/5 = 0.8 \)

Ellipse with b/a=1/10;  \( e = \sqrt{1-1/100} = 0.995 \) approximately

Ellipse with b=0 and a finite;  e = 1

We can get specific ellipsoid models using almanac

```
almanac
Parameters for Earth, planets, Sun, and Moon

Syntax

almanac
almanac(budy)
data = almanac(budy,parameter)
data = almanac(budy,parameter,units)
data = almanac(parameter,units,referencebody)

Description

almanac is not recommended. Use earthRadius, referenceEllipsoid, referenceSphere, or wgs84Ellipsoid instead.

Almanac (perhaps) being phased out in 2012 version, but still functioning
```

```
>> distance(35,-80,36,-81) % spherical earth
ans = 1.2895 degrees

>> distance(35,-80,36,-81,almanac('earth','wgs84','degrees'))
ans = 1.2889 degrees

>> distance(35,-80,36,-81,almanac('earth','wgs84','meters'))
ans = 1.4332e+05 meters

>> distance(35,-80,36,-81,almanac('earth','wgs84','km'))
ans = 143.3216 km
```
A couple other ways to get topography & bathymetry: GeoMapApp

3. Save as GMT3 grid

4. Use grid2d.m to read the data (on class m-files page)

http://www.marine-geo.org/portals/gmrt/
grdread2 read in as NODE registered GMT data

```matlab
>> [X,Y,Z]=grdread2('canrockies_gmt3.grd');
>> whos
Name      Size          Bytes  Class         Attributes
X         1x723         5784   double
Y         1x475         3800   double
Z        475x723       1373709 single
```

dx=mode(diff(X)); % = 0.00439
dy=mode(diff(Y)); % = 0.0026

```matlab
R=makerefmat(X(1),Y(1),dx,dy)
R =
 0.00439   0
-120.744   51.680
```

Actual Header File Info:
```
grdinfo2('canrockies_gmt3.grd')
Gridline node registration used
x_min: -120.739746094
x_max: -117.566894531
x_inc: 0.00439453125
name: Longitude nx: 723

y_min: 51.6834549965
y_max: 52.9565806756
y_inc: 0.00268591915434
name: Latitude ny: 475

We can check that our R matrix return the correct result
```
[X,Y,Z]=grdread2('canrockies_gmt3.grd');
dx=mode(diff(X));
dy=mode(diff(Y));
Z=double(Z); % make into a floating point value
R=makerefmat(X(1),Y(1),dx,dy);
figure; axesm('MapProjection','mercator');
contourfm(Z,R,3,'k')
```
setm(gca, 'MapLatLimit', [min(Y) max(Y)], 'MapLonLimit', [min(X) max(X)])
setm(gca, 'ParallelLabel', 'on', 'MeridianLabel', 'on', 'Grid', 'on', 'LabelUnits', 'dm')
setm(gca, 'MLabelLocation', 45/60, 'PLabelLocation', 10/60)
tightmap; colorbar('vert');

**Terrain Analysis:**
Digital estimation of the slope, aspect, and curvatures of terrain data.

**Leading to:** terrain classification, flow path analysis, catchment delineation, solar radiation, channel lines, line of sight calculation.

Mapping toolbox function: gradientm
\[ \text{[aspect, slope, gradN, gradE]} = \text{gradientm}(Z, R) \]
Computes the slope, aspect and north and east components of the gradient for a regular data grid \( Z \) with 1x3 referencing vector or 3x2 reference matrix (if \( x \) and \( y \) grid spacing are different).

If the grid contains elevations in meters, the resulting aspect and slope are in units of **degrees clockwise from north and up from the horizontal**.

The north and east gradient components are the change in the map variable per meter of distance in the north and east directions.

\( [...] = \text{gradientm}(\text{lat}, \text{lon}, Z) \)
\( \text{lat and lon} \) are the latitudes and longitudes of the geo-located points, and are in degrees.

\([X,Y,Z]=\text{grdread2('grid3\_rs.grd')}\);
\( Z=\text{double}(Z); \ dx=\text{mode}(\text{diff}(X)); \ dy=\text{mode}(\text{diff}(Y)); \)
\( R=\text{makerefmat}(X(1),Y(1),dx,dy) \) % spacing not equal

figure; axesm('MapProjection', 'mercator');
\( \text{meshm}(Z,R); \text{view}(0,90); \text{caxis}([\text{min}(Z(:)),\text{max}(Z(:))]); \)
\( \text{contourm}(Z,R,10,'k'); \)
setm(gca, 'MapLatLimit', [min(Y) max(Y)], 'MapLonLimit', [min(X) max(X)])
setm(gca, 'ParallelLabel', 'on', 'MeridianLabel', 'on', 'Grid', 'on', 'LabelUnits', 'dm')
setm(gca, 'MLabelLocation', 5/60, 'PLabelLocation', 5/60)
tightmap; colorbar('vert');

**Terrain Analysis Example**
Flanks of Mid Atlantic Ridge
[aspect, slope, gradN, gradE] = gradientm(Z, R); % does all the calculations

[LAT, LON] = meshgrat(Z, R); % need for surfm

figure; axesm('MapProjection', 'mercator');
surfm(LAT, LON, slope);
setm(gca, 'MapLatLimit', [min(Y) max(Y)], 'MapLonLimit', [min(X) max(X)])
setm(gca, 'ParallelLabel', 'on', 'MeridianLabel', 'on', 'LabelUnits', 'dm')
setm(gca, 'MLabelLocation', 5/60, 'PLabelLocation', 5/60)
setm(gca, 'MlineLocation', 5/60, 'PLineLocation', 5/60)
tightmap; colorbar('vert');
figure;
v=2:4.54;
c=isnan(slope);
hist(slope(~c),v); xlim([0,50])
xlabel('slope'); ylabel('number of points')