

## HINT FOR HW #1

- Problem 1. You need to find three sets of the solutions, or three sub-questions. Note that, for the last one, it may have no solution indicating that we need more points to get a consistent finite difference formula.
- Problem 2. Consider both the stability and consistency. Is the boundary condition used in the scheme?
- Suggestions for Problem 3. You can use Maple or Matlab symbolic function to find  $f(x)$ . Write separate matlab function u.m, du.m. For example, you can edit a text file called u.m with

```
function y = u(x)
y = exp(-x)*(x-1)^2;
```

Note that you should NOT use beta.m since beta is a Matlab built-in function. Instead, you can use my\_beta.m

```
function y = my_beta(x)
y = (1+x*x);
```

You can write a matlab script file, say *my\_main.m* as we did in class

```
n=80;
a=2; b=-3;
c = a*u(1) + b*du(1);
....
```

Note that, the parameters  $a$ ,  $b$ , and  $c$  really should be  $\alpha$ ,  $\beta$ , and  $\gamma$  using the notations in my notes; and  $\beta(x)$  should be  $p(x)$ .

The ghost point method for the mixed boundary condition should be

$$aU_n + b\frac{U_{n+1} - U_{n-1}}{2h} = c$$

from which you solve for  $U_{n+1}$  and plug it into the 3-point central finite difference equation at  $x = x_n$ .

For the programming part of the HW, you should arrange, edit your outputs, plots using the following format:

- The problem. What do we know and what do we want to find.
- The numerical method along with any derivation if there is any.
- Results and analysis. Please label your plots, tables, etc.
- Analysis and conclusions that you can get from your results.

*The purpose of this process is to start write papers or technical reports. It is important for you to submit your compute codes, that is, those .m files to Wolfware.*