

Creep and Stress Rupture :

Ch. 13 : 3, 4, 5, 6, 7, 8, 9, 11, 12, 13, 15(optional)

- **Definition of Creep and Creep Curve : (13-3)**

- def. *Creep is the time-dependent plastic strain at constant stress and temperature*

Creep curve : Fig. 13-4

- steady-state creep-rate ($\dot{\epsilon}_s$ or simply $\dot{\epsilon}$) : Temperature and Stress Dependencies
- Fig. 13-6 Fig. 13-8

- total creep curve : $\epsilon = \epsilon_0 + \epsilon_p + \epsilon_s$

ϵ_0 = instantaneous strain at loading (elastic, anelastic and plastic)

ϵ_s = steady-state creep strain (constant-rate *viscous creep*) = $\dot{\epsilon}_s t$

ϵ_p = primary or transient creep : Andrade- β flow (or 1/3 rd law) : $\beta t^{1/3}$

primary or transient creep :

- Andrade- β flow (or 1/3 rd law) : $\epsilon_p = \beta t^{1/3} \Leftrightarrow$ problem as $t \rightarrow 0$
- Garofalo / Dorn Equation : $\epsilon_p = \epsilon_t (1 - e^{-rt})$, r is related to $\frac{\dot{\epsilon}_i}{\dot{\epsilon}_s}$ (~1-20)

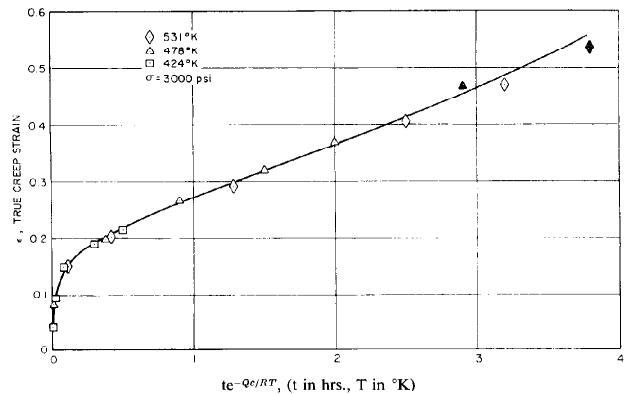
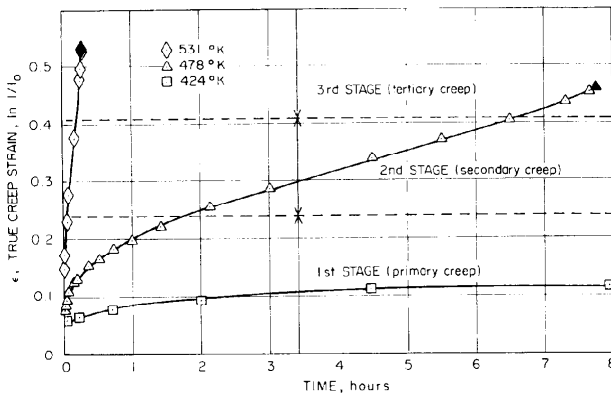
Dorn \Rightarrow Both primary and steady-state follow similar kinetics

- temperature compensated time ($\theta = t e^{-Q_c/RT}$)

- single universal curve with t replaced by θ or $\dot{\epsilon}_s t$

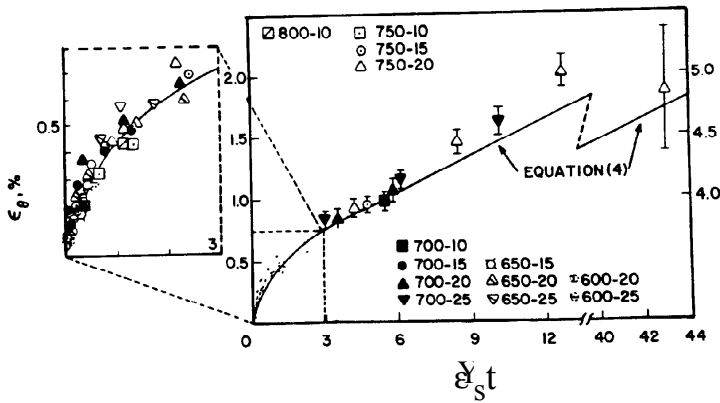
Or, creep strain $\epsilon - \epsilon_0 = \epsilon_t (1 - e^{-\dot{\epsilon}_s t}) + \dot{\epsilon}_s t \Leftrightarrow$ see Sherby-Dorn (Al), Murty (Zr)

Sherby-Dorn θ -parameter

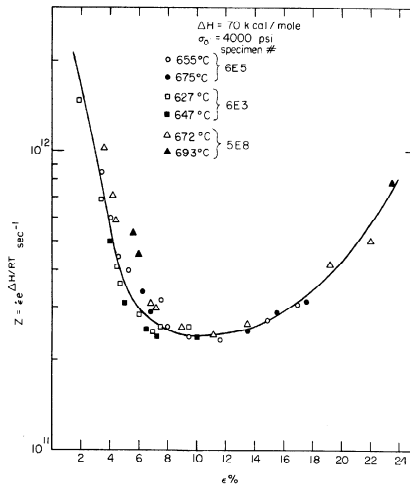


Creep curves for Al at Sherby & Dorn (1956) (3,000 psi) and at three different temperatures

A single curve demonstrating the validity of θ -parameter



Creep data in Zircaloy at varied temperatures (°F) and stresses (ksi) fall into a single curve demonstrating the validity of Dorn equation (Murty et al 1976)



(K. L. Murty, M.S. Thesis, 1967)

• Zener-Holloman : $Z = \dot{\epsilon} e^{Q/RT}$

- **Stress Rupture Test** : (13-4) σ vs t_r
- **Representation of engineering creep / rupture data** (13-12, 13-13) - Figs. 13-17, 13-18

• Sherby-Dorn Parameter : $P_{S-D} = t e^{-Q/RT}$

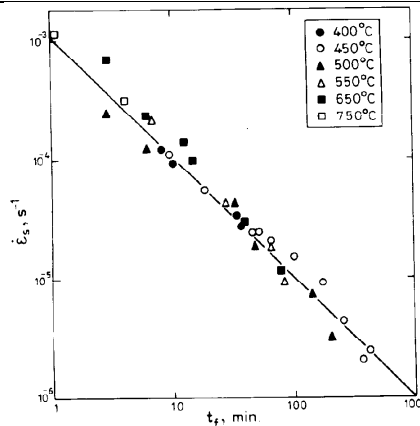
• Larson-Miller Parameter : $P_{L-M} = T (\log t + C)$ Fig. 13-19-21

• Manson-Haferd Parameter : $P_{M-H} = \frac{T - T_a}{\log t - \log t_a}$

--- these parameters are for a given stress and are functions of σ (Fig. 13-20) ---

• Monkman-Grant : $\dot{\epsilon}_s t_r = K$

Eq. 13-24



Demonstration of Monkman-Grant Relationship in Cu (Feltham and Meakin 1959)

Creep Under Multiaxial Loading

(text 14-14)

Use Levy-Mises Equations in plasticity

$$\sigma_{\text{eff}} = \frac{1}{\sqrt{2}} \sqrt{(\sigma_1 - \sigma_2)^2 + (\sigma_2 - \sigma_3)^2 + (\sigma_3 - \sigma_1)^2}$$

and $d\epsilon_1 = \frac{d\epsilon_{\text{eff}}}{\sigma_{\text{eff}}} \left[\sigma_1 - \frac{1}{2}(\sigma_2 + \sigma_3) \right]$,

since creep is plastic deformation 1/2 appears as in plasticity.

Similarly, $d\epsilon_2$ and $d\epsilon_3$.

Dividing by dt, get the corresponding creep-rates,

$$\dot{\epsilon}_1 = \frac{\dot{\epsilon}_{\text{eff}}}{\sigma_{\text{eff}}} \left[\sigma_1 - \frac{1}{2}(\sigma_2 + \sigma_3) \right], \text{ etc.}$$

One first determines the uniaxial creep-rate equation,

$$\dot{\epsilon}_s = A \sigma^n e^{-Q/RT}$$

and assume the same for effective strain-rate : $\dot{\epsilon}_{\text{eff}} = A \sigma_{\text{eff}}^n e^{-Q/RT}$

so that $\dot{\epsilon}_1 = A \sigma_{\text{eff}}^{n-1} e^{-Q/RT} \left[\sigma_1 - \frac{1}{2}(\sigma_2 + \sigma_3) \right]$ etc.

Stress Relaxation

As noted in section 8-11, the stress relaxation occurs when the deformation is held constant such as in bolt in flange where the constraint is that **the total length of the system is fixed**.

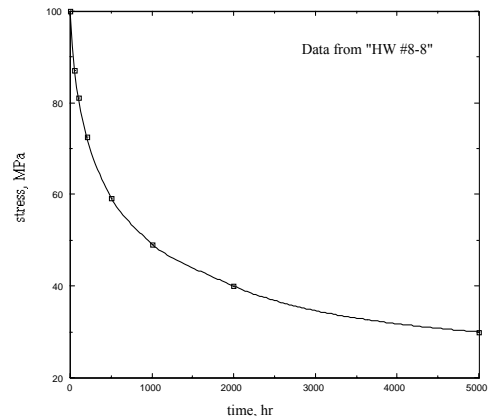
$\epsilon_t = \epsilon_E + \epsilon_{\text{creep}} = \text{const.}$ Here, $\epsilon_E = \frac{\sigma}{E}$.

Thus $\frac{d\epsilon_t}{dt} = 0 = \frac{1}{E} \frac{d\sigma}{dt} + \dot{\epsilon}_s$ Or, $\frac{d\sigma}{dt} = -E \dot{\epsilon}_s = -E A \sigma^n$ @ fixed T

Integration from 0 to t gives,

$$\int_{\sigma_i}^{\sigma_f} \frac{d\sigma}{\sigma^n} = -E A \int_0^t dt = -E A t$$

$$\sigma_{\text{final}} \text{ or } \sigma(t) = \frac{\sigma_o}{[1 + AE(n-1)\sigma_o^{n-1}t]^{1/(n-1)}}$$



- **Deformation / Creep Mechanisms :**
 - Introduction - structural changes (13-5)
 - Slip (difficult to observe slip lines / folds etc are usually noted)
 - Subgrains
 - GBS
 - excess (deformation induced) vacancies

- Two important relationships :

Orowan equation : $\dot{\epsilon} = \rho b v$ and Taylor equation : $\rho = \frac{\sigma^2}{\alpha^2 G^2 b^2}$

- **Thermally Activated Dislocation Glide** (at low T and/or high strain-rates)

$\dot{\epsilon} = A e^{B\sigma} e^{-Q_i/RT}$ where Q_i is the activation energy for the underlying mechanisms

Peierls mechanism (bcc metals) Intersection mechanism (fcc and hcp metals)

- **Dislocation creep** - (lattice) diffusion controlled glide and climb
- **Diffusion creep** - (viscous creep mechanisms mainly due to point defects) - at low stresses and high temperatures
- **Grain-Boundary Sliding** - (GBS) - intermediate stresses in small grained materials and ceramics (where matrix deformation is difficult)
- Many different mechanisms may contribute and the total strain-rate :

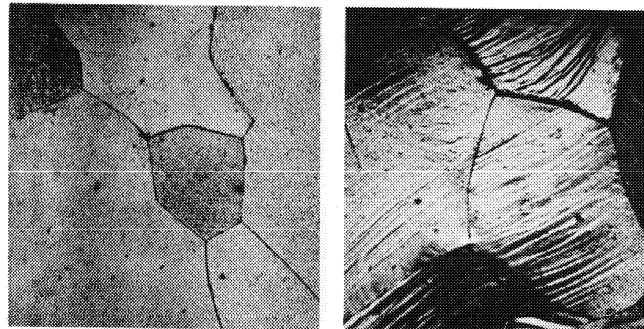
parallel mechanism
(fastest controls / dominates)

$$\dot{\epsilon} = \sum_i \dot{\epsilon}_i$$

series mechanisms
(slower controls / dominates)

$$\dot{\epsilon} = \sum \left(\frac{1}{\dot{\epsilon}_i} \right)^{-1}$$

Slip following creep deformation in α -iron



Uncrept specimen

Crept at 5500 psi to 21.5% strain

(K.L. Murty, MS thesis, Cornell University, 1967)

- **Dislocation Creep :**

- Pure Metals / Class-M alloys: Experiments : $\dot{\epsilon} = A \sigma^n e^{-Q_c/RT}$, $n \approx 5$, $Q_c \approx Q_L$ (Q_D)

(edge \perp) glide - climb model *Weertman-Climb model* (Weertman Pill-Box Model)

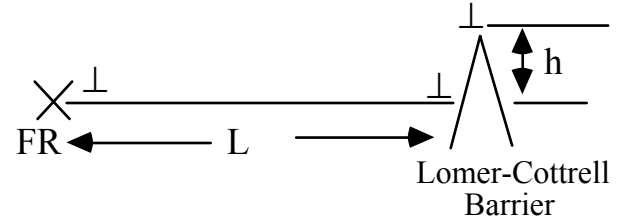
- *sequential processes*

L = average distance a dislocation glides

t_g = time for glide motion

h = average distance a dislocation climbs

t_c = time for climb



$$\Delta\gamma = \text{strain during glide-climb event} = \Delta\gamma_g + \Delta\gamma_c \approx \Delta\gamma_g = \rho b L$$

$$t = \text{time of glide-climb event} = t_g + t_c \approx t_c = \frac{h}{v_c}, \quad v_c = \text{climb velocity}$$

$$\therefore \dot{\gamma} = \frac{\Delta\gamma}{t} = \frac{\rho b L}{h/v_c} = \rho b \left(\frac{L}{h}\right) v_c$$

where $v_c \propto \Delta C_v e^{-E_m/kT}$, E_m = activation energy for vacancy migration

$$\text{Here, } \Delta C_v = C_v^+ - C_v^- = C_v^0 e^{\sigma V/kT} - C_v^0 e^{-\sigma V/kT} = C_v^0 2 \text{ Sinh}\left(\frac{\sigma V}{kT}\right)$$

$$\therefore \dot{\epsilon} = \alpha \rho b \left(\frac{L}{h}\right) v_c = \alpha \rho b \left(\frac{L}{h}\right) C_v^0 e^{-E_m/kT} 2 \text{ Sinh}\left(\frac{\sigma V}{kT}\right)$$

At low stresses, $\text{Sinh}(\xi) \approx \xi$ so that

$$\dot{\epsilon} = A_1 \rho b \left(\frac{L}{h}\right) C_v^0 e^{-E_m/kT} \frac{\sigma V}{kT}$$

$$\dot{\epsilon} = A_1 \rho b \left(\frac{L}{h}\right) D_L \frac{\sigma V}{kT} \approx A_2 \rho \sigma \left(\frac{L}{h}\right) D_L$$

Or $\dot{\epsilon} = A \sigma^3 D \Leftrightarrow$ *natural creep-law*

Weertman: $\frac{L}{h} \propto \sigma^{1.5}$, $\dot{\epsilon} = A \sigma^{4.5} D$ as

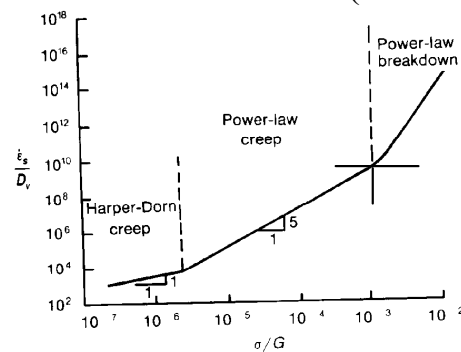
experimentally observed in Al

In general $\dot{\epsilon} = A(T) \sigma^n$ Power-law

- n is the stress exponent

{f(xal structure, Γ)}

Garofalo Eqn.
 $\dot{\epsilon} = A D (\sinh B\sigma)^n$



also known as Norton's Equation
(n is Norton index)

At high stresses ($\sigma \geq 10^{-3} E$), $\text{Sinh}(x) \approx e^x$, $\dot{\epsilon} = A_H e^{B\sigma} D$ (Power-law breakdown)

Experimental Observations - Dislocation Creep

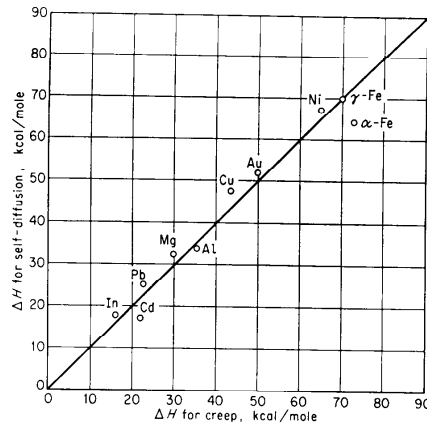
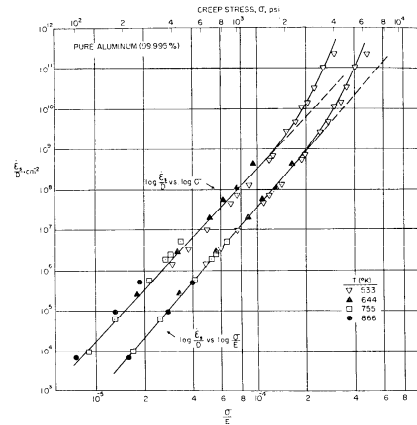


Fig. 13-13 (Dieter)



(Sherby)

What happens if we keep decreasing the stress, say to a level at and below the τ_{FR} ?

As σ is decreased \Rightarrow reach a point when $\sigma \leq \sigma_{FR}$,

dislocation density would become constant (independent of σ): $\dot{\epsilon} \propto \sigma$

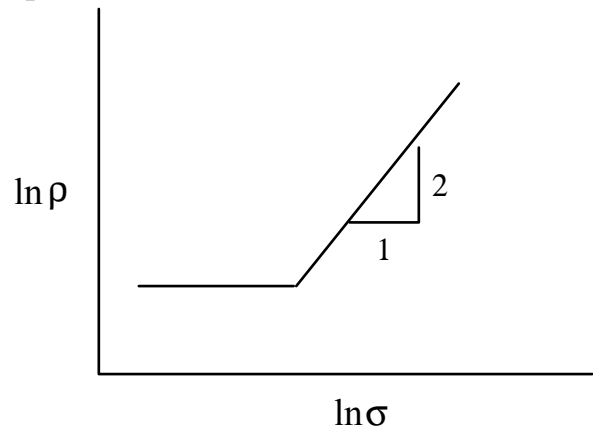
- viscous creep known as Harper-Dorn creep

Harper-Dorn creep occurs at

$$\frac{\sigma}{E} \leq b \sqrt{\rho_0} \approx 10^{-5}, \quad \rho_0 \approx 10^6 \text{ cm}^{-2}$$

- H-D creep is observed in **large** grained materials (metals, ceramics, etc.)

$$\dot{\epsilon}_{HD} = A_{HD} D_L \sigma$$



Characteristics of Climb Creep (Class-M) :

- large primary creep regions
- subgrain formation ($\delta \propto \frac{1}{\sigma}$)
- dislocation density $\propto \sigma^2$
- independent of grain size

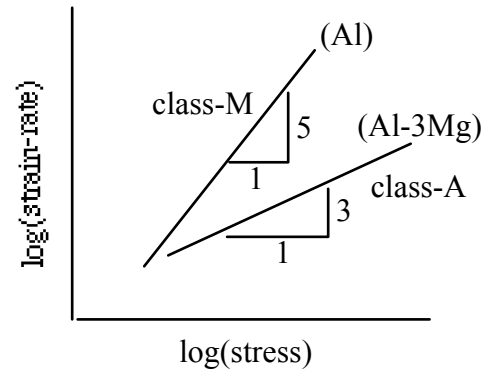
- **Effects of Alloying : (class-A)**

- Solid-solution - decreases rate of glide \uparrow glide controlled creep although annihilation due to climb still occurs (*micro-creep / viscous glide creep*)

viscous glide controlled creep : (decreased creep-rates)

$$\dot{\epsilon}_g = A_g D_s \sigma^3, \quad D_s \text{ is solute diffusion}$$

- little or no primary creep
- **no** subgrain formation
- $\rho \propto \sigma^2$
- grain-size independent



- At low stresses (for large grain sizes), Harper-Dorn creep dominates
 \Rightarrow what happens as grain size becomes small \Leftarrow

As grain-size **decreases** (and at low stresses) diffusion creep due to point defects becomes important : (due to migration of vacancies from tensile boundaries to compressive boundaries)

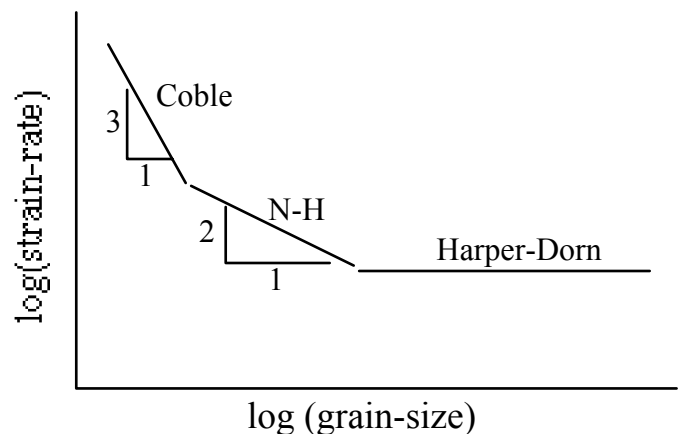
- Nabarro-Herring Creep (diffusion through the lattice) : $\dot{\epsilon}_{NH} = A_{NH} D_L \frac{\sigma}{d^2}$
- Coble Creep (diffusion through grain-boundaries) : $\dot{\epsilon}_{Co} = A_{Co} D_b \frac{\sigma}{d^3}$

Nabarro-Herring Creep vs Coble Creep :

Coble creep for small grain sizes and at low temperature

NH creep for larger grain sizes and at high temperatures

- at very large grain sizes, Harper-Dorn creep dominates



At small grain-sizes, GBS dominates at intermediate stresses and temperatures :

- $\dot{\epsilon}_{GBS} = A_{GBS} D_b \frac{\sigma^2}{d^2} \Leftrightarrow \textit{superplasticity}$

- Effect of dispersoids : Dispersion Strengthening / Precipitate Hardening
 - recall Orowan Bowing
- at high temperatures, climb of dislocation loops around the precipitates controls creep $\Rightarrow \dot{\epsilon}_{ppt} = A_{ppt} D \sigma^{8-20}$

Rules for Increasing Creep Resistance

- Large Grain Size
(directionally solidified superalloys)
- Low Stacking Fault Energy
(Cu vs Cu-Al alloys)
- Solid Solution Alloying
(Al vs Al-Mg alloys)
- Dispersion Strengthening
(Ni vs TD-Ni)

Formability Improvement

- Small (stable) Equiaxed Grain Size
(superplasticity)
- Strengthen Matrix
(i.e., increase GBS - ceramics)
- Stoichiometry
(especially Ceramics)

Summary of Creep Mechanisms: $\dot{\epsilon}_t = \dot{\epsilon}_{N-H} + \dot{\epsilon}_{Coble} + \dot{\epsilon}_{H-D} + \dot{\epsilon}_{GBS} + \left(\frac{1}{\dot{\epsilon}_c} + \frac{1}{\dot{\epsilon}_g} \right)^{-1}$

$$\text{Dorn Equation : } \frac{\dot{\epsilon}kT}{DEb} = A \left(\frac{\sigma}{E} \right)^n$$

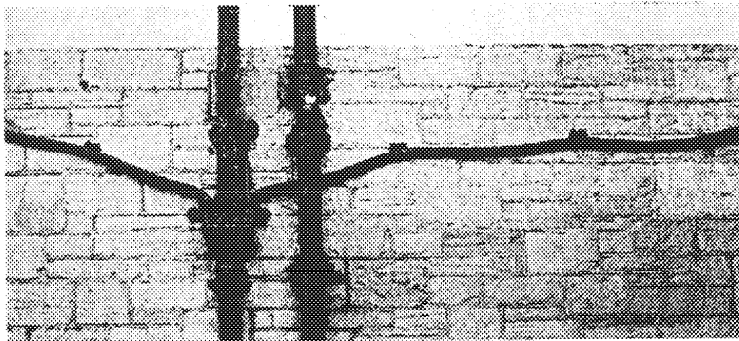
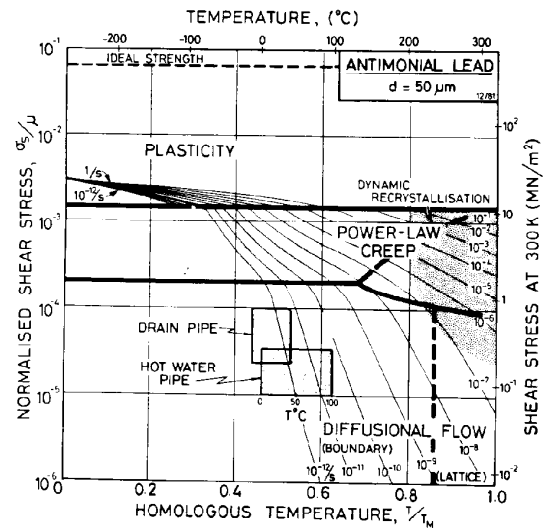
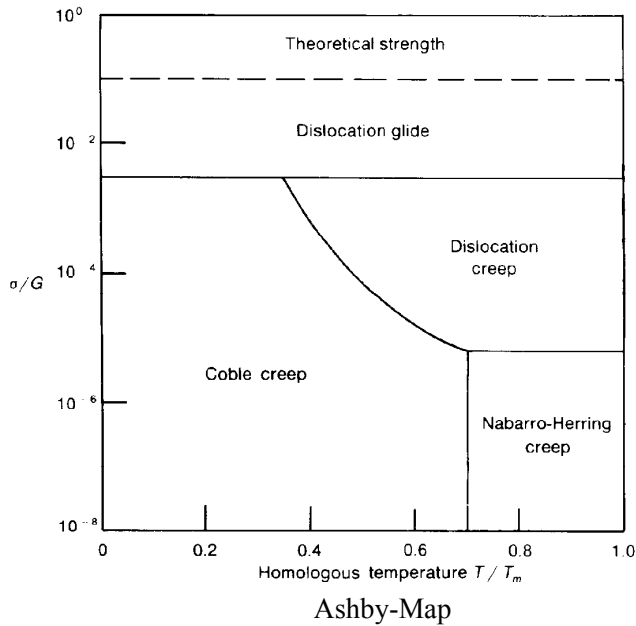
Mechanism	D	n	A
Climb of edge dislocations (Pure Metals and class-M alloys)	D_L	5	6×10^7
Low-temperature climb	D_{\perp}	7	2×10^8
Viscous glide (Class-I alloys - microcreep)	D_s	3	6
Nabarro-Herring	D_L	1	$14 \left(\frac{b}{d} \right)^2$
Coble	D_b	1	$100 \left(\frac{b}{d} \right)^3$
Harper-Dorn	D_L	1	3×10^{-10}
GBS (superplasticity)	D_b	2	$200 \left(\frac{b}{d} \right)^2$

D_L = lattice diffusivity; D_s = solute diffusivity; D_{\perp} = core diffusivity;
 D_b = Grain-Boundary Diffusivity; b = Burgers vector; d = grain size;
 δ = subgrain size = $10 \frac{Gb}{\tau}$ and $\rho = \frac{\sigma^2}{G^2 b^2}$ where G is the shear modulus

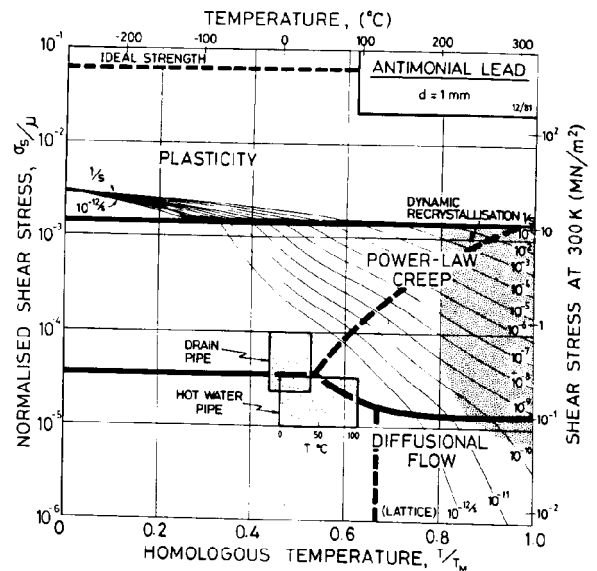
*n increases with decreasing Γ (stacking-fault energy)

Deformation Mechanism Maps

- Visual picture of the domains (σ , T) where various mechanisms dominate



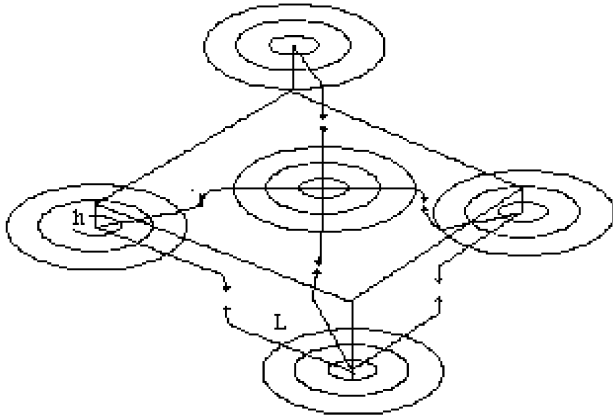
Lead pipes on a 75-year-old building in southern England
The creep-induced curvature of these pipes is typical of Victorian lead water piping. (Frost and Ashby)



Other examples :

- W filament (light bulbs)
- turbid blade {Ni-based alloy DS by $\text{Ni}_3(\text{Ti},\text{Al})$ }

WEERTMAN PILL-BOX MODEL



Pure Metals - Glide faster
Climb-controlled creep ($n \approx 5$)

$$\dot{\epsilon}_t = \left(\frac{1}{\dot{\epsilon}_c} + \frac{1}{\dot{\epsilon}_g} \right)^{-1}$$

Alloys - Glide slower
Glide-controlled creep ($n \approx 3$)

Solid Solution Alloys

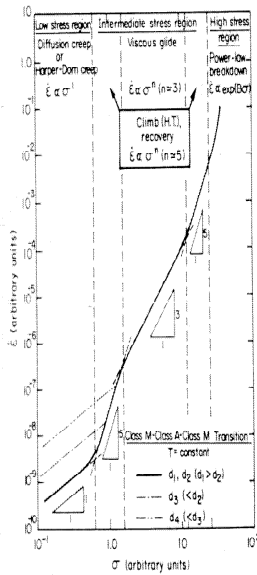


Fig. 9 Schematic illustration of logarithmic strain rate versus logarithmic stress for solid solution alloys.

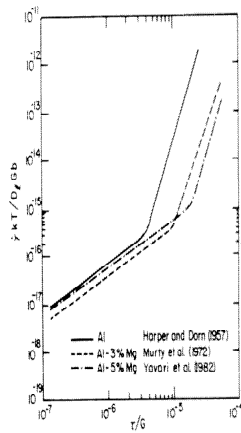
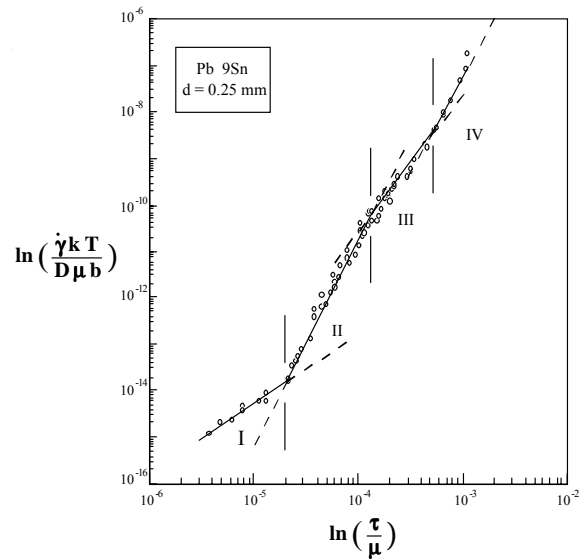


Fig. 10 Temperature compensated shear strain rate versus normalized shear stress for pure Al and two Al-Mg alloys.



Murty and Turlik (1992)

Creep Transitions for Alloy Class