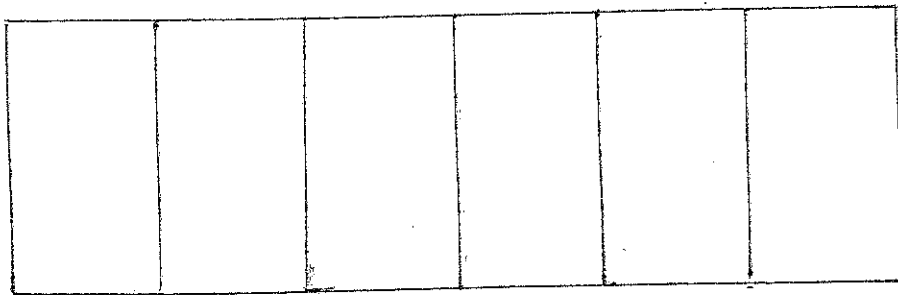


Please put all work and answers in the stamped blue book provided. Do not use a calculator that does calculus - show your work to justify your answers. Simplify all derivatives completely. Put your name, form of test (A, B, or C), row letter, and seat number on the front of the blue book.

1.) Find  $y'$ :  $y = (e^{x^2} - 5)^3$

2.) A veterinarian has 120 feet of fencing and wishes to construct six dog kennels by first building a fence around a rectangular region, and then subdividing that region into six smaller rectangles by placing five fences parallel to one of the sides. What dimensions of the region will maximize the total area?



3.) Evaluate the indefinite integral:  $\int (6x^2 - 7x^{\frac{2}{3}} + \frac{9}{x} + 8x^{-3} - 5e^{3x}) dx$

4.) Find  $y'$ :  $y = \ln(8x^2 - 3)$

5.) The number of women graduating from 4-year colleges in the United States has grown exponentially from 1930, when 48,800 women earned such a degree, to 2005, when 832,500 women received such a degree. Use this data to predict the number of degrees that women will receive in 2013.

6.) Find the exact area (using a definite integral) of the region under the curve  $y = 16 - x^2$  from  $x = -4$  to  $x = 4$ .

7.) Find  $y'$ : a.)  $y = 6^{x^2+3}$  b.)  $y = \log_8(x^2 - x)$

8.) The temperature in a hot tub is  $104^\circ$ , and the room temperature is  $73^\circ$ . The water cools to  $97^\circ$  in 15 minutes. Using Newton's Law of Cooling ( $T = ae^{kt} + M$ ), determine the amount of time it would take for the water to cool to  $83^\circ$ .

3 problems; 12 pts each

1.)  $y = (e^{x^2} - 5)^3$

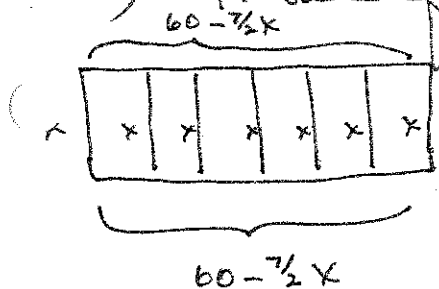
$$y' = 3(e^{x^2} - 5)^2 \cdot d(e^{x^2} - 5)$$

$$y' = 3(e^{x^2} - 5)^2 \cdot (e^{x^2}) \cdot d(x^2)$$

$$y' = 3(e^{x^2} - 5)^2 \cdot (e^{x^2}) \cdot (2x)$$

$$y' = 6x \cdot e^{x^2} \cdot (e^{x^2} - 5)^2$$

2.) total fence: 120 ft.



$$\frac{120 - 7x}{2} = 60 - \frac{7}{2}x$$

$$A = x \left(60 - \frac{7}{2}x\right)$$

$$A = 60x - \frac{7}{2}x^2$$

$$A' = 60 - \frac{7}{2}(2x) = 60 - 7x = 0$$

$$60 = 7x \quad x = \frac{60}{7} \approx 8.57$$

other side:  $60 - \frac{7}{2}\left(\frac{60}{7}\right) = 60 - 30 = 30$

$$A'' = -7 \text{ (always NEG; } \therefore \text{ c. DOWN, } \therefore \text{ max)}$$

$$\text{dimensions: } \frac{60}{7} \text{ ft by } 30 \text{ ft}$$

$$\approx 8.57$$

T3C (page 2)

$$3.) \int (6x^2 - 7x^{2/3} + \frac{9}{x} + 8x^{-3} - 5e^{3x}) dx$$

$$= 6 \cdot \left(\frac{x^3}{3}\right) - 7 \left(\frac{x^{5/3}}{5/3}\right) + 9 \int \frac{1}{x} dx + 8 \left(\frac{x^{-2}}{-2}\right) - 5 \left(\frac{1}{3} e^{3x}\right) + C$$

$$= 2x^3 - \frac{21}{5} x^{5/3} + 9 \cdot \ln|x| - 4x^{-2} - \frac{5}{3} e^{3x} + C$$

$$4.) y = \ln(8x^2 - 3) \quad y' = \frac{1}{8x^2 - 3} \cdot d(8x^2 - 3)$$

$$y' = \frac{16x}{8x^2 - 3}$$

$$(\cdot) y = y_0 \cdot e^{kt}$$

$$t=0 (1930) \quad \left\{ \begin{array}{l} t=75 (2005) \\ t=83 (2013) \end{array} \right. \quad \left\{ \begin{array}{l} y=48,800 \\ y=832,500 \\ y=? \end{array} \right.$$

$$y = 48,800 e^{kt}$$

$$(y_0 = 48,800)$$

$$t=75 \quad y=832,500 \quad 832,500 = 48,800 e^{k \cdot 75}$$

$$\frac{832,500}{48,800} = e^{75k}$$

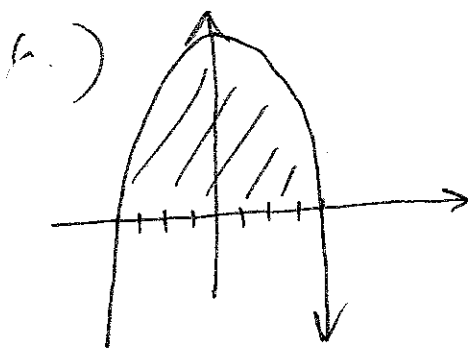
$$\ln\left(\frac{832,500}{48,800}\right) = 75k$$

$$k = \frac{\ln\left(\frac{832,500}{48,800}\right)}{75} \approx .037823$$

$$y = 48,800 e$$

$$t=83 \quad y=?$$

$$y = 48,800 \cdot e^{(.037823)(83)} \approx 1,126,662$$



(graph not necessary)

$$A = \int_{-4}^4 (16 - x^2) dx$$

$$= \left[ 16x - \frac{x^3}{3} \right]_{-4}^4$$

$$= \left[ 16(4) - \frac{4^3}{3} \right] - \left[ 16(-4) - \frac{(-4)^3}{3} \right]$$

$$= \left[ 64 - \frac{64}{3} \right] - \left[ -64 + \frac{64}{3} \right]$$

$$= 64 + 64 - \frac{64}{3} - \frac{64}{3} = 128 - \frac{128}{3}$$

$$A = \frac{384}{3} - \frac{128}{3} = \frac{256}{3} = 85\frac{1}{3} \approx 85.33$$

7.) a.)  $y = 6^{x^2+3}$   $y' = 6^{x^2+3} \cdot (\ln 6) (2x)$

b.)  $y = \log_8(x^2-x)$   $y' = \frac{1}{(x^2-x) \cdot \ln 8} \cdot (2x-1)$

$$y' = \frac{2x-1}{(x^2-x) \cdot \ln 8}$$

8.)  $T = a \cdot e^{kt} + m$   $\left\{ \begin{array}{l} t=0 \\ T=104^\circ \end{array} \right\} \left\{ \begin{array}{l} t=15 \\ T=97^\circ \end{array} \right\} \left\{ \begin{array}{l} t=? \\ T=83^\circ \end{array} \right.$   
 $(m=73^\circ)$

$t=0 \rightarrow 104 = a \cdot e^{k(0)} + 73$   $104 - 73 = a$   $a = 31$

$T = 31e^{kt} + 73$   $\left\{ \begin{array}{l} t=15 \\ T=97 \end{array} \right. \rightarrow 97 = 31e^{k \cdot 15} + 73$   $97 - 73 = 31e^{k \cdot 15}$   
 $\frac{97-73}{31} = e^{k \cdot 15}$   $\ln\left(\frac{97-73}{31}\right) = 15k$   
 $k = \frac{\ln\left(\frac{97-73}{31}\right)}{15} \approx -0.017062$   
 $83 = 31e^{-0.017062t} + 73$   $\frac{10}{31} = e^{-0.017062t}$   $\ln\left(\frac{10}{31}\right) = -0.017062t$   $t = \frac{\ln\left(\frac{10}{31}\right)}{-0.017062} \approx 66.3$  min