

North Carolina State University  
MA 242 Section 008 Exam 1

Read all directions carefully. **A graphing calculator may NOT be used on this exam.** You must Show All Work for credit and clearly indicate your final answer; no work equals no credit. When you are finished fold your exam, write your name on the outside, turn it in, and then you may leave quietly. Good Luck!

- 1) For the vectors  $\vec{v} = \langle 2, \frac{-1}{3}, 1 \rangle$  and  $\vec{u} = \langle 6, 3, 0 \rangle$  compute the following.
  - a) (6 pts)  $\vec{u} \cdot \vec{v}$
  - b) (6 pts)  $\vec{u} \times \vec{v}$ .
  - c) (6 pts) Are the vectors perpendicular, parallel, or neither? Give reasons for your answer.
  
- 2) a) (10 pts) Find the equation of the line through the point  $(1, -5, 7)$  that is parallel to the line given by the vector equation  $\langle 7 + 2t, -1 + t, -t \rangle$ .  
  
b) (14 pts) Find the equation of the plane that contains the line  $\langle 7 + 2t, -1 + t, -t \rangle$  and the point  $(2, -1, -1)$ .
  
- 3) (16 pts) Find the position vector of a particle that has acceleration  $\vec{a}(t) = ti + e^tj + e^{-t}k$ , initial velocity  $\vec{v}(0) = j - k$ , and initial position  $\vec{r}(0) = i + j + 2k$ .
  
- 4) The vector equation of a circle of radius  $a$  in two dimensions is  $\vec{r}(t) = a \cos(t)i + a \sin(t)j$ .
  - a) (12 pts) Find the unit normal vector  $N$  to the curve.
  - b) (12 pts) Calculate the curvature  $\kappa$ .
  
- 5) Given  $\vec{u}_1$  and  $\vec{u}_2$  are orthogonal unit vectors,  $\vec{a} = a_1u_1 + a_2u_2$ , and  $\vec{b} = b_1u_1 + b_2u_2$  compute the following.
  - a) (6 pts)  $\vec{a} \cdot \vec{u}_1$
  - b) (6 pts)  $\vec{a} \cdot \vec{b}$
  - c) (6 pts)  $\vec{u}_1 \cdot (\vec{u}_1 \times \vec{a})$  give reasons for your answer.

**BONUS**

In real number multiplication when  $a \neq 0$  and  $ab = ac$  this implies  $b=c$ .

- a) (3 pts) Show this is not true for the dot product. Find vectors  $\vec{a}, \vec{b}, \vec{c}$  such that  $\vec{a} \neq \vec{0}$  and  $\vec{a} \cdot \vec{b} = \vec{a} \cdot \vec{c}$  but  $\vec{b} \neq \vec{c}$ .
- b) (2 pts) There is also no such rule for cross products. Find vectors  $\vec{a}, \vec{b}, \vec{c}$  such that  $\vec{a} \neq \vec{0}$  and  $\vec{a} \times \vec{b} = \vec{a} \times \vec{c}$  but  $\vec{b} \neq \vec{c}$ .