

Differential Equation Model.

$$y(t + dt) - y(t) \approx dt * c * (y_{sur} - y(t)).$$

dt = change in time

c = insulation proportionality constant

y_{sur} = given surrounding temperature

$y(t)$ = temperature.

Let dt go to zero to get

$$y' = c(y_{sur} - y).$$

Method of Solution.

Use the substitution method $z = y_{\text{sur}} - y$.

For example,

$$y' = (1/26)(70.0 - y) \text{ and } y(0) = 200.$$

Let $z = 70. - y$ to get

$$-z' = (1/26)z \text{ and } z(0) = 70 - 200 = -130.$$

$$\text{So, } z(t) = -130e^{(-t/26)} \text{ and } y(t) = 70 + 130e^{(-t/26)}.$$

Matlab Implementation.

1. Use function file temp.m

```
function temp = temp(t)  
temp = 70 + 130*exp(-t/26);
```

Now the temperature function can be easily evaluated:

```
EDU» temp(1)  
ans =  
195.0949
```

```
EDU» temp(2)  
ans =  
190.3749
```

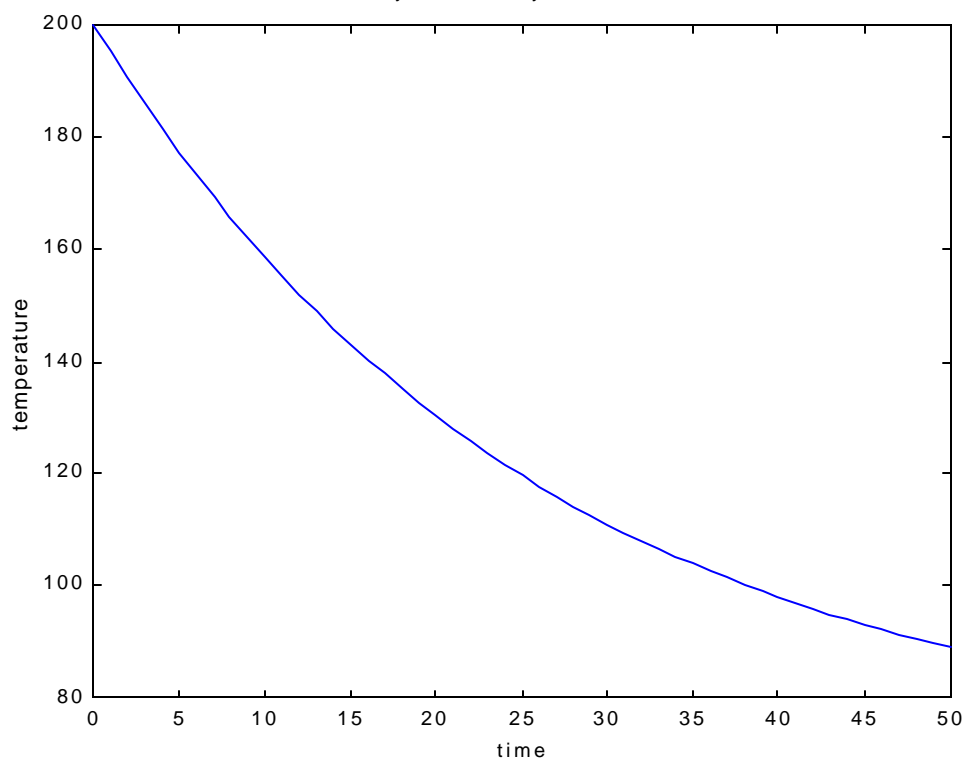
2. Use loops.

```
EDU» clear;           % This clears the memory.

EDU» for i = 0:50     % This starts the loop.
time(i+1) = i;
y(i+1) = temp(i);
end

EDU» plot(time,y)     % Plots the graph.
EDU» title('Lesson 1, your name, your student
number')
EDU» xlabel('time')
EDU» ylabel('temperature')
```

Lesson 1, your name, your student number



3. Use m-file cooling.m.

```
% Lesson 1, your name, your student number  
clear; % This clears the memory.  
for i = 0:50 % This starts the loop from time  
= 0 to 50.  
  
    time(i+1) = i;  
    y(i+1) = temp(i);  
end  
plot(time,y) % Plots the graph and inserts  
title and labels.  
  
title('Lesson 1, your name, your student number')  
xlabel('time')  
ylabel('temperature')
```

Now the above calculations can be executed by a single command at the Matlab prompt by just typing cooling.